

V5.0

# Function Catalog



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## IMSL C NUMERICAL LIBRARY

*Written in C for C / C++ programmers and based on the world's most widely called numerical subroutines.*

The IMSL C Numerical Library ("CNL") is a comprehensive set of over 370 pre-built mathematical and statistical analysis functions that C or C++ programmers can embed directly into their numerical analysis applications. Many of CNL's functions are based upon the same algorithms contained in the company's highly regarded IMSL Fortran 90 MP Library. Visual Numerics, Inc. has been providing algorithms for mathematical and statistical computations under the IMSL name since 1970.

With CNL, we provide "building blocks" which eliminate the need to write code from scratch. These prepackaged functions allow you to apply your industry-specific expertise and reduce your development time.

CNL takes full advantage of the intrinsic characteristics and desirable features of the C language. Variable argument lists simplify calling sequences. The concise set of required arguments contains only information necessary for usage. Optional arguments provide added functionality and power to each function.

CNL is thread safe. Thread safety allows CNL to be used in multithreaded applications ranging from web-based applications to performing advanced data analysis in real time. Which gives you increased throughput, better response time, conservation of system resources and a natural programming structure. Performance benefits can be realized through concurrent and/or parallel execution.

CNL has also been designed to take advantage of symmetric multiprocessor (SMP) systems. Computationally intensive algorithms in areas such as linear algebra and fast Fourier transforms will leverage SMP capabilities on a variety of systems. By allowing you to replace the generic Basic Linear Algebra Subprograms ("BLAS") contained in CNL with optimized BLAS from your hardware vendor, you can improve the performance of your numerical calculations.

You can build applications that are portable across multiple platforms. CNL is available for computer systems running UNIX and Windows operating systems.

Extensive online documentation provides powerful search capabilities with hundreds of code examples.

Rely on the industry leader for software that is expertly developed, thoroughly tested, meticulously maintained and well documented. Get reliable results **EVERY TIME!**

## **COST-EFFECTIVENESS AND VALUE**

CNL significantly shortens program development time and promotes standardization. Variable argument lists have been implemented to simplify calling sequences. You'll find that using CNL saves time in your source code development and saves thousands of dollars in the design, development, documentation, testing and maintenance of your applications.

## **ACCURATE, ROBUST AND RELIABLE**

CNL uses descriptive, explanatory function names for intuitive programming. Reserved function names begin with prefixes unique to each product.

Where appropriate, consistent variable names are used to:

- Make function names easy to identify and use and prevent conflicts with other software.
- Provide a common root name for numerical functions that offers the choice of multiple precisions.

## **ERROR HANDLING**

Diagnostic error messages are clear and informative - designed not only to convey the error condition but also to suggest corrective action if appropriate.

These error-handling features:

- Make it faster and easier for you to debug your programs.
- Provide for more productive programming and confidence that the algorithms are functioning properly in your application.

## **PROGRAMMING INTERFACE FLEXIBILITY**

CNL takes full advantage of the intrinsic characteristics and desirable features of the C language. The functions support variable-length argument lists. The concise set of required arguments contains only information necessary for usage. Optional arguments provide added functionality and power to each function.

This flexibility:

- Reduces unnecessary code.
- Enables you to adapt each function call by activating optional arguments.

## **WIDE COMPATIBILITY AND UNIFORM OPERATION**

The IMSL C Numerical Library is available for UNIX computing environments and Windows 98/2000/NT.

Visual Numerics' commitment to regular feature and enhancement updates:

- Ensures that your software will perform to the highest standards.
- Provides for portable applications.
- Assures that Visual Numerics will keep pace with the latest hardware and software innovations.

## SHARED LIBRARY TECHNOLOGY

The IMSL C Numerical Library is designed to take advantage of shared libraries technology.

This technology:

- Allows more than one user to share information in the library without crowding disk space.
- Provides shorter compile and link time.
- Minimizes the size of executable object modules.

## FLEXIBLE LICENSING OPTIONS

The IMSL C Numerical Library can be licensed in a number of flexible ways: licenses may be node-locked to a specific CPU, or a specified number of licenses can be purchased to "float" throughout a heterogeneous network as they are needed. This allows you to cost-effectively acquire as many seats as you need today, adding more seats when it becomes necessary. Site licenses and campus licenses are also available.

## COMPREHENSIVE DOCUMENTATION

Documentation for CNL is comprehensive, clearly written and standardized. Detailed information about each function is found in a single source within a chapter and consists of section name, purpose, synopsis, required and optional arguments, errors, return values and usage examples. Each manual's alphabetical index enables convenient cross-referencing.

IMSL extensive documentation:

- Provides organized, easy-to-find information.
- Documents, explains, and provides references for algorithms.
- Gives at least one example of function usage, with sample input and results.

## UNMATCHED PRODUCT SUPPORT

Behind every Visual Numerics' license is a team of professionals ready to provide expert answers to questions about your IMSL software. Product support options include product maintenance and consultation, ensuring value and performance of your IMSL software.

Product support:

- Gives you direct access to Visual Numerics' resident staff of expert product support specialists.
- Provides prompt, two-way communication with solutions to your programming needs.
- Includes product maintenance updates.

## MATHEMATICAL FUNCTIONALITY

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The IMSL C Numerical Library is a collection of the most commonly needed numerical functions customized for your C programming needs. The mathematical functionality is organized into 10 sections. These capabilities range from solving systems of linear equations to optimization.

- **Linear Systems**, including real and complex full and sparse matrices, linear least squares, matrix decompositions, generalized inverses and vector-matrix operations.
- **Eigensystem Analysis**, including eigenvalues and eigenvectors of complex, real symmetric and complex Hermitian matrices.
- **Interpolation and Approximation**, including constrained curve-fitting splines, cubic splines, least squares approximation and smoothing, and scattered data interpolation.
- **Integration and Differentiation**, including univariate, multivariate and Gauss quadrature.
- **Differential Equations**, using Adams-Gear and Runge-Kutta methods for stiff and nonstiff ordinary differential equations and support for partial differential equations.
- **Transforms**, including real and complex one- and two-dimensional fast Fourier transforms, as well as convolutions and correlations and Laplace transforms.
- **Nonlinear Equations**, including zeros and root finding of polynomials, zeros of a function and root of a system of equations.
- **Optimization**, including unconstrained, and linearly and nonlinearly constrained minimizations.
- **Special Functions**, including error and gamma functions, real order complex valued Bessel functions, statistical functions, and more than fifty functions for financial analysis.
- **Utilities**, including CPU time used, error handling and machine, mathematical, physical constants, retrieval of machine constants, changing error-handling defaults, and performing matrix-matrix multiplication.

## STATISTICAL FUNCTIONALITY

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The statistical functionality is organized into 12 sections. These capabilities range from analysis of variance to random number generation.

- **Basic Statistics**, including univariate summary statistics, nonparametric tests, such as sign and Wilcoxon rank sum, and goodness-of-fit tests, such as chi-squared and Shapiro-Wilk.
- **Regression**, including stepwise regression, all best regression, multiple linear regression models, polynomial models and nonlinear models.
- **Correlation and Covariance**, including sample variance-covariance, partial correlation and covariances, pooled variance-covariance and robust estimates of a covariance matrix and mean factor.
- **Analysis of Variance**, including one-way classification models, a balanced factorial design with fixed effects and the Student-Newman-Keuls multiple comparisons test.
- **Categorical and Discrete Data Analysis**, including chi-squared analysis of a two-way contingency table, exact probabilities in a two-way contingency table and analysis of categorical data using general linear models.
- **Nonparametric Statistics**, including sign tests, Wilcoxon sum tests and Cochran Q test for related observations.
- **Tests of Goodness-of-Fit**, including chi-squared goodness-of-fit tests, Kolmogorov/Smirnov tests and tests for normality.
- **Time Series Analysis and Forecasting**, including analysis and forecasting of time series using a nonseasonal ARMA model, GARCH (Generalized Autoregressive Conditional Heteroskedasticity), Kalman filtering, portmanteau lack of fit test and difference of a seasonal or nonseasonal time series.
- **Multivariate Analysis**, including principal components, K-means cluster analysis and factor analysis. Methods of factor analysis include principal components, principal factor, image analysis, unweighted least squares, generalized least squares and maximum likelihood.
- **Survival Analysis**, including analysis of data using a generalized linear model and using various parametric models.
- **Probability Distribution Functions and Inverses**, including binomial, hypergeometric, bivariate normal, gamma and many more.
- **Random Number Generation**, including a generator for multivariate normal distributions and pseudorandom numbers from several distributions, including gamma, Poisson and beta. Also, support for low discrepancy series using a generalized Faure sequence.

# IMSL<sup>®</sup> C Numerical Library<sup>®</sup>

## Functions

IMSL C/Math/Library<sup>™</sup>

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### CHAPTER 1: LINEAR SYSTEMS

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#### LINEAR EQUATIONS WITH FULL MATRICES

##### **lin\_sol\_gen**

Solves a real general system of linear equations  $Ax = b$ .

##### **lin\_sol\_gen (complex)**

Solves a complex general system of linear equations  $Ax = b$ .

##### **lin\_sol\_posdef**

Solves a real symmetric positive definite system of linear equations  $Ax = b$ .

##### **lin\_sol\_posdef (complex)**

Solves a complex Hermitian positive definite system of linear equations  $Ax = b$ .

#### LINEAR EQUATIONS WITH BAND MATRICES

##### **lin\_sol\_gen\_band**

Solves a real general band system of linear equations  $Ax = b$ .

##### **lin\_sol\_gen\_band (complex)**

Solves a complex general band system of linear equations  $Ax = b$ .

##### **lin\_sol\_posdef\_band**

Solves a real symmetric positive definite system of linear equations  $Ax = b$  in band symmetric storage mode.

##### **lin\_sol\_posdef\_band (complex)**

Solves a complex Hermitian positive definite system of linear equations  $Ax = b$  in band symmetric storage mode.

#### LINEAR EQUATIONS WITH GENERAL SPARSE MATRICES

##### **lin\_sol\_gen\_coordinate**

Solves a sparse system of linear equations  $Ax = b$ .

##### **lin\_sol\_gen\_coordinate (complex)**

Solves a sparse Hermitian positive definite system of linear equations  $Ax = b$ , with sparse complex coefficient matrix  $A$ .

##### **lin\_sol\_posdef\_coordinate**

Solves a sparse real symmetric positive definite system of linear equations  $Ax = b$ .

##### **lin\_sol\_posdef\_coordinate (complex)**

Solves a sparse Hermitian positive definite system of linear equations  $Ax = b$ .

#### ITERATIVE METHODS

##### **lin\_sol\_gen\_min\_residual**

Solves a linear system  $Ax = b$  using the restarted generalized minimum residual (GMRES) method.

##### **lin\_sol\_def\_cg**

Solves a real symmetric definite linear system using a conjugate gradient method.

#### LINEAR LEAST-SQUARES WITH FULL MATRICES

##### **lin\_least\_squares\_gen**

Solves a linear least-squares problem  $Ax = b$ .

##### **lin\_lsq\_lin\_constraints**

Solves a linear least squares problem with linear constraints.

##### **lin\_svd\_gen**

Computes the SVD,  $A = USV^T$ , of a real rectangular matrix  $A$ .

##### **lin\_svd\_gen (complex)**

Computes the SVD,  $A = USV^H$ , of a complex rectangular matrix  $A$ .

##### **lin\_sol\_nonnegdef**

Solves a real symmetric nonnegative definite system of linear equations  $Ax = b$ .

### CHAPTER 2: EIGENSYSTEM ANALYSIS

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#### LINEAR EIGENSYSTEM PROBLEMS

##### **eig\_gen**

Computes the eigenexpansion of a real matrix  $A$ .

##### **eig\_gen (complex)**

Computes the eigenexpansion of a complex matrix  $A$ .

##### **eig\_sym**

Computes the eigenexpansion of a real symmetric matrix  $A$ .

##### **eig\_herm (complex)**

Computes the eigenexpansion of a complex Hermitian matrix  $A$ .

#### GENERALIZED EIGENSYSTEM PROBLEMS

##### **eig\_symgen**

Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ .  $A$  and  $B$  are real and symmetric.  $B$  is positive definite.

##### **geneig**

Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ , with  $A$  and  $B$  real.

##### **geneig (complex)**

Computes the generalized eigenexpansion of a system  $Ax = \lambda Bx$ , with  $A$  and  $B$  complex.



## CHAPTER 3: INTERPOLATION AND APPROXIMATION

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### CUBIC SPLINE INTERPOLATION

#### **cub\_spline\_interp\_e\_cnd**

Computes a cubic spline interpolant, specifying various endpoint conditions.

#### **cub\_spline\_interp\_shape**

Computes a shape-preserving cubic spline.

### CUBIC SPLINE EVALUATION AND INTEGRATION

#### **cub\_spline\_value**

Computes the value of a cubic spline or the value of one of its derivatives.

#### **cub\_spline\_integral**

Computes the integral of a cubic spline.

### SPLINE INTERPOLATION

#### **spline\_interp**

Computes a spline interpolant.

#### **spline\_knots**

Computes the knots for a spline interpolant.

#### **spline\_2d\_interp**

Computes a two-dimensional, tensor-product spline interpolant from two-dimensional, tensor-product data.

### SPLINE EVALUATION AND INTEGRATION

#### **spline\_value**

Computes the value of a spline or the value of one of its derivatives.

#### **spline\_integral**

Computes the integral of a spline.

#### **spline\_2d\_value**

Computes the value of a tensor-product spline or the value of one of its partial derivatives.

#### **spline\_2d\_integral**

Evaluates the integral of a tensor-product spline on a rectangular domain.

### LEAST-SQUARES APPROXIMATION AND SMOOTHING

#### **user\_fcn\_least\_squares**

Computes a least-squares fit using user-supplied functions.

#### **spline\_least\_squares**

Computes a least-squares spline approximation.

#### **spline\_2d\_least\_squares**

Computes a two-dimensional, tensor-product spline approximant using least squares.

#### **cub\_spline\_smooth**

Computes a smooth cubic spline approximation to noisy data by using cross-validation to estimate the smoothing parameter or by directly choosing the smoothing parameter.

#### **spline\_lsq\_constrained**

Computes a least-squares constrained spline approximation.

#### **smooth\_1d\_data**

Smooth one-dimensional data by error detection.

### SCATTERED DATA INTERPOLATION

#### **scattered\_2d\_interp**

Computes a smooth bivariate interpolant to scattered data that is locally a quintic polynomial in two variables.

### SCATTERED DATA LEAST SQUARES

#### **radial\_scattered\_fit**

Computes an approximation to scattered data in  $\mathbf{R}^n$  for  $n \geq 2$  using radial basis functions.

#### **radial\_evaluate**

Evaluates a radial basis fit.

## CHAPTER 4: QUADRATURE

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### UNIVARIATE QUADRATURE

#### **int\_fcn\_sing**

Integrates a function, which may have endpoint singularities, using a globally adaptive scheme based on Gauss-Kronrod rules.

#### **int\_fcn**

Integrates a function using a globally adaptive scheme based on Gauss-Kronrod rules.

#### **int\_fcn\_sing\_pts**

Integrates a function with singularity points given.

#### **int\_fcn\_alg\_log**

Integrates a function with algebraic-logarithmic singularities.

#### **int\_fcn\_inf**

Integrates a function over an infinite or semi-infinite interval.

#### **int\_fcn\_trig**

Integrates a function containing a sine or a cosine factor.

#### **int\_fcn\_fourier**

Computes a Fourier sine or cosine transform.

#### **int\_fcn\_cauchy**

Computes integrals of the form  $\int_a^b \frac{f(x)}{x-c} dx$  in the Cauchy principal value sense.

#### **int\_fcn\_smooth**

Integrates a smooth function using a nonadaptive rule.

## MULTIVARIATE QUADRATURE

### **int\_fcn\_2d**

Computes a two-dimensional iterated integral.

### **int\_fcn\_hyper\_rect**

Integrates a function on a hyper-rectangle

$$\int_{a_0}^{b_0} \cdots \int_{a_{n-1}}^{b_{n-1}} f(x_0, \dots, x_{n-1}) dx_{n-1} \cdots dx_0.$$

### **int\_fcn\_qmc**

Integrates a function on a hyper-rectangle using a quasi-Monte-Carlo method.

## GAUSS QUADRATURE

### **gauss\_quad\_rule**

Computes a Gauss, Gauss-Radau, or Gauss-Lobatto quadrature rule with various classical weight functions.

## DIFFERENTIATION

### **fcn\_derivative**

Computes the first, second or third derivative of a user-supplied function.

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## CHAPTER 5: DIFFERENTIAL EQUATIONS

## RUNGE-KUTTA METHOD

### **ode\_runge\_kutta**

Solves an initial-value problem for ordinary differential equations using the Runge-Kutta-Verner fifth-order and sixth-order method.

## ADAM'S OR GEAR'S METHOD

### **ode\_adams\_gear**

Solves a stiff initial-value problem for ordinary differential equations using the Adams-Gear methods.

## METHOD OF LINES

### **pde\_method\_of\_lines**

Solves a system of partial differential equations of the form  $u_t = f(x, t, u, u_x, u_{xx})$  using the method of lines.

## FAST POISSON SOLVER

### **fast\_poisson\_2d**

Solves Poisson's or Helmholtz's equation on a two-dimensional rectangle using a fast Poisson solver based on the HODIE finite-difference scheme on a uniform mesh.

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## CHAPTER 6: TRANSFORMS

## REAL TRIGONOMETRIC FFTS

### **fft\_real**

Computes the real discrete Fourier transform of a real sequence.

### **fft\_real\_init**

Computes the parameters for `imsl_f_fft_real`.

## COMPLEX EXPONENTIAL FFTS

### **fft\_complex**

Computes the complex discrete Fourier transform of a complex sequence.

### **fft\_complex\_init**

Computes the parameters for `imsl_c_fft_complex`.

## REAL SINE AND COSINE FFTS

### **fft\_cosine**

Computes the discrete Fourier cosine transformation of an even sequence.

### **fft\_cosine\_init**

Computes the parameters needed for `imsl_f_fft_cosine`.

### **fft\_sine**

Computes the discrete Fourier sine transformation of an odd sequence.

### **fft\_sine\_init**

Computes the parameters needed for `imsl_f_fft_sine`.

## TWO-DIMENSIONAL FFTS

### **fft\_2d\_complex**

Computes the complex discrete two-dimensional Fourier transform of a complex two-dimensional array.

## CONVOLUTION AND CORRELATION

### **convolution**

Computes the convolution, and optionally, the correlation of two real vectors.

### **convolution (complex)**

Computes the convolution, and optionally, the correlation of two complex vectors.

## LAPLACE TRANSFORM

### **inverse\_laplace**

Computes the inverse Laplace transform of a complex function.

## CHAPTER 7: NONLINEAR EQUATIONS

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### ZEROS OF A POLYNOMIAL

#### **zeros\_poly**

Finds the zeros of a polynomial with real coefficients using the Jenkins-Traub three-stage algorithm.

#### **zeros\_poly (complex)**

Finds the zeros of a polynomial with complex coefficients using the Jenkins-Traub three-stage algorithm.

### ZEROS OF A FUNCTION

#### **zeros\_fcn**

Finds the real zeros of a real function using Müller's method.

### ROOT OF A SYSTEM OF EQUATIONS

#### **zeros\_sys\_eqn**

Solves a system of  $n$  nonlinear equations  $f(x) = 0$  using a modified Powell hybrid algorithm.

## CHAPTER 8: OPTIMIZATION

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### UNCONSTRAINED MINIMIZATION

#### **min\_uncon**

Finds the minimum point of a smooth function  $f(x)$  of a single variable using only function evaluations.

#### **min\_uncon\_deriv**

Finds the minimum point of a smooth function  $f(x)$  of a single variable using both function and first derivative evaluations.

#### **min\_uncon\_multivar**

Minimizes a function  $f(x)$  of  $n$  variables using a quasi-Newton method.

#### **nonlin\_least\_squares**

Solves a nonlinear least-squares problem using a modified Levenberg-Marquardt algorithm.

### LINEARLY CONSTRAINED MINIMIZATION

#### **lin\_prog**

Solves a linear programming problem using the revised simplex algorithm.

#### **quadratic\_prog**

Solves a quadratic programming problem subject to linear equality or inequality constraints.

#### **min\_con\_gen\_lin**

Minimizes a general objective function subject to linear equality/inequality constraints.

#### **bounded\_least\_squares**

Solves a nonlinear least-squares problem subject to bounds on the variables using a modified Levenberg-Marquardt algorithm.

### NONLINEARLY UNCONSTRAINED MINIMIZATION

#### **min\_con\_nonlin**

Solves a general nonlinear programming problem using the successive quadratic programming algorithm.

## CHAPTER 9: SPECIAL FUNCTIONS

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### ERROR AND GAMMA FUNCTIONS

#### **erf**

Evaluates the real error function  $\text{erf}(x)$ .

#### **erfc**

Evaluates the real complementary error function  $\text{erfc}(x)$ .

#### **erf\_inverse**

Evaluates the real inverse error function  $\text{erf}^{-1}(x)$ .

#### **erfc\_inverse**

Evaluates the real inverse complementary error function  $\text{erfc}^{-1}(x)$ .

#### **beta**

Evaluates the real beta function  $\beta(x, y)$ .

#### **log\_beta**

Evaluates the logarithm of the real beta function  $\ln \beta(x, y)$ .

#### **beta\_incomplete**

Evaluates the real incomplete beta function  $I_x = \beta_x(a, b) / \beta(a, b)$ .

#### **gamma**

Evaluates the real gamma function  $\Gamma(x)$ .

#### **log\_gamma**

Evaluates the logarithm of the absolute value of the gamma function  $\log |\Gamma(x)|$ .

#### **gamma\_incomplete**

Evaluates the incomplete gamma function  $\gamma(a, x)$ .

### BESSEL FUNCTIONS

#### **bessel\_J0**

Evaluates the real Bessel function of the first kind of order zero  $J_0(x)$ .

#### **bessel\_J1**

Evaluates the real Bessel function of the first kind of order one  $J_1(x)$ .

#### **bessel\_Jx**

Evaluates a sequence of Bessel functions of the first kind with real order and complex arguments.

#### **bessel\_Y0**

Evaluates the real Bessel function of the second kind of order zero  $Y_0(x)$ .

**bessel\_Y1**

Evaluates the real Bessel function of the second kind of order one  $Y_1(x)$ .

**bessel\_Yx**

Evaluates a sequence of Bessel functions of the second kind with real order and complex arguments.

**bessel\_I0**

Evaluates the real modified Bessel function of the first kind of order zero  $I_0(x)$ .

**bessel\_exp\_I0**

Evaluates the exponentially scale modified Bessel function of the first kind of order zero.

**bessel\_I1**

Evaluates the real modified Bessel function of the first kind of order one  $I_1(x)$ .

**bessel\_exp\_I1**

Evaluates the exponentially scaled modified Bessel function of the first kind of order one.

**bessel\_lx**

Evaluates a sequence of modified Bessel functions of the first kind with real order and complex arguments.

**bessel\_K0**

Evaluates the real modified Bessel function of the third kind of order zero  $K_0(x)$ .

**bessel\_exp\_K0**

Evaluates the exponentially scaled modified Bessel function of the third kind of order zero.

**bessel\_K1**

Evaluates the real modified Bessel function of the third kind of order one  $K_1(x)$ .

**bessel\_exp\_K1**

Evaluates the exponentially scaled modified Bessel function of the third kind of order one.

**bessel\_Kx**

Evaluates a sequence of modified Bessel functions of the third kind with real order and complex arguments.

**ELLIPTIC INTEGRALS****elliptic\_integral\_K**

Evaluates the complete elliptic integral of the kind  $K(x)$ .

**elliptic\_integral\_E**

Evaluates the complete elliptic integral of the second kind  $E(x)$ .

**elliptic\_integral\_RF**

Evaluates Carlson's elliptic integral of the first kind  $R_F(x, y, z)$ .

**elliptic\_integral\_RD**

Evaluates Carlson's elliptic integral of the second kind  $R_D(x, y, z)$ .

**elliptic\_integral\_RJ**

Evaluates Carlson's elliptic integral of the third kind  $R_J(x, y, z, \rho)$ .

**elliptic\_integral\_RC**

Evaluates an elementary integral from which inverse circular functions, logarithms, and inverse hyperbolic functions can be computed.

**FRESNEL INTEGRALS****fresnel\_integral\_C**

Evaluates the cosine Fresnel integral.

**fresnel\_integral\_S**

Evaluates the sine Fresnel integral.

**AIRY FUNCTIONS****airy\_Ai**

Evaluates the Airy function.

**airy\_Bi**

Evaluates the Airy function of the second kind.

**airy\_Ai\_derivative**

Evaluates the derivative of the Airy function.

**airy\_Bi\_derivative**

Evaluates the derivative of the Airy function of the second kind.

**KELVIN FUNCTIONS****kelvin\_ber0**

Evaluates the Kelvin function of the first kind, ber, of order zero.

**kelvin\_bei0**

Evaluates the Kelvin function of the first kind, bei, of order zero.

**kelvin\_ker0**

Evaluates the Kelvin function of the second kind, ker, of order zero.

**kelvin\_kei0**

Evaluates the Kelvin function of the second kind, kei, of order zero.

**kelvin\_ber0\_derivative**

Evaluates the derivative of the Kelvin function of the first kind, ber, of order zero.

**kelvin\_bei0\_derivative**

Evaluates the derivative of the Kelvin function of the first kind, bei, of order zero.

**kelvin\_ker0\_derivative**

Evaluates the derivative of the Kelvin function of the second kind, ker, of order zero.

**kelvin\_kei0\_derivative**

Evaluates the derivative of the Kelvin function of the second kind, kei, of order zero.

## STATISTICAL FUNCTIONS

### **normal\_cdf**

Evaluates the standard normal (Gaussian) distribution function.

### **normal\_inverse\_cdf**

Evaluates the inverse of the standard normal (Gaussian) distribution function.

### **chi\_squared\_cdf**

Evaluates the chi-squared distribution function.

### **chi\_squared\_inverse\_cdf**

Evaluates the inverse of the chi-squared distribution function.

### **F\_cdf**

Evaluates the  $F$  distribution function.

### **F\_inverse\_cdf**

Evaluates the inverse of the  $F$  distribution function.

### **t\_cdf**

Evaluates the Student's  $t$  distribution function.

### **t\_inverse\_cdf**

Evaluates the inverse of the Student's  $t$  distribution function.

### **gamma\_cdf**

Evaluates the gamma distribution function.

### **binomial\_cdf**

Evaluates the binomial distribution function.

### **hypergeometric\_cdf**

Evaluates the hypergeometric distribution function.

### **poisson\_cdf**

Evaluates the Poisson distribution function.

### **beta\_cdf**

Evaluates the beta probability distribution function.

### **beta\_inverse\_cdf**

Evaluates the inverse of the beta distribution function.

### **bivariate\_normal\_cdf**

Evaluates the bivariate normal distribution function.

## FINANCIAL FUNCTIONS

### **cumulative\_interest**

Evaluates the cumulative interest paid between two periods.

### **cumulative\_principal**

Evaluates the cumulative principal paid between two periods.

### **depreciation\_db**

Evaluates the depreciation of an asset. (Fixed-declining-balance method).

### **depreciation\_ddb**

Evaluates the depreciation of an asset. (Double-declining-balance method).

### **depreciation\_sln**

Evaluates the depreciation of an asset. (Straight-line method).

### **depreciation\_synd**

Evaluates the depreciation of an asset. (Sum-of-years digits method).

### **depreciation\_vdb**

Evaluates the depreciation of an asset for any given period, including partial periods. (Double-declining-balance method).

### **dollar\_decimal**

Converts a fractional price to a decimal price.

### **dollar\_fraction**

Converts a decimal price to a fractional price.

### **effective\_rate**

Evaluates the effective annual interest rate.

### **future\_value**

Evaluates an investment's future value.

### **future\_value\_schedule**

Evaluates the future value of an initial principal taking into consideration a schedule of compound interest rates.

### **interest\_payment**

Evaluates the interest payment for an investment for a given period.

### **interest\_rate\_annuity**

Evaluates an annuity's interest rate per period.

### **internal\_rate\_of\_return**

Evaluates the internal rate of return for a schedule of cash flows.

### **internal\_rate\_schedule**

Evaluates the internal rate of return for a schedule of cash flows. It is not necessary that the cash flows be periodic.

### **modified\_internal\_rate**

Evaluates the modified internal rate of return for a schedule of periodic cash flows.

### **net\_present\_value**

Evaluates an investment's net present value. The calculation is based on a schedule of periodic cash flows and a discount rate.

### **nominal\_rate**

Evaluates the nominal annual interest rate.

### **number\_of\_periods**

Evaluates the number of periods for an investment for which periodic and constant payments are made and the interest rate is constant.

### **payment**

Evaluates the periodic payment for an investment.

**present\_value**

Evaluates an investment's present value.

**present\_value\_schedule**

Evaluates the present value for a schedule of cash flows. It is not necessary that the cash flows be periodic.

**principal\_payment**

Evaluates the payment on the principal for a specified period.

**BOND FUNCTIONS****accr\_interest\_maturity**

Evaluates the interest that has accrued on a security, which pays interest at maturity.

**accr\_interest\_periodic**

Evaluates the interest that has accrued on a security, which pays interest periodically.

**bond\_equivalent\_yield**

Evaluates a Treasury bill's bond-equivalent yield.

**convexity**

Evaluates the convexity for a security.

**coupon\_days**

Evaluates the number of days in the coupon period containing the settlement date.

**coupon\_number**

Evaluates the number of coupons payable between the settlement date and the maturity date.

**days\_before\_settlement**

Evaluates the number of days starting with the beginning of the coupon period and ending with the settlement date.

**days\_to\_next\_coupon**

Evaluates the number of days starting with the settlement date and ending with the next coupon date.

**depreciation\_amordegrc**

Evaluates the depreciation for each accounting period. During the evaluation of the function a depreciation coefficient based on the asset life is applied.

**depreciation\_amorlinc**

Evaluates the depreciation for each accounting period. This function is similar to depreciation\_amordegrc, except that depreciation\_amordegrc has a depreciation coefficient that is applied during the evaluation that is based on the asset life.

**discount\_price**

Evaluates a discounted security's price per \$100 face value.

**discount\_rate**

Evaluates a security's discount rate.

**discount\_yield**

Evaluates a discounted security's annual yield.

**duration**

Evaluates a security's annual duration where the security has periodic interest payments.

**interest\_rate\_security**

Evaluates a fully invested security's interest rate.

**modifiedmacauley\_duration**

Evaluates a security's modified Macauley duration. The security has an assumed par value of \$100.

**next\_coupon\_date**

Evaluates the first coupon date that follows the settlement date.

**previous\_coupon\_date**

Evaluates the coupon date that immediately precedes the settlement date.

**price**

Evaluates a security's price per \$100 face value. The security pays periodic interest.

**price\_maturity**

Evaluates a security's price per \$100 face value. The security pays interest at maturity.

**received\_maturity**

Evaluates the amount one receives when a fully invested security reaches the maturity date.

**treasury\_bill\_price**

Evaluates a Treasury bill's price per \$100 face value.

**treasury\_bill\_yield**

Evaluates a Treasury bill's yield.

**year\_fraction**

Evaluates the fraction of a year represented by the number of whole days between two dates.

**yield\_maturity**

Evaluates a security's annual yield. The security pays interest at maturity.

**yield\_periodic**

Evaluates a security's yield. The security pays periodic interest.

## **CHAPTER 10: STATISTICS AND RANDOM NUMBER GENERATION**

---

**STATISTICS****simple\_statistics**

Computes basic univariate statistics.

**table\_oneway**

Tallies observations into a one-way frequency table.

**chi\_squared\_test**

Performs a chi-squared goodness-of-fit test.

**covariances**

Computes the sample variance-covariance or correlation matrix.

**regression**

Fits a multiple linear regression model using least squares.

**poly\_regression**

Performs a polynomial least-squares regression.

**ranks**

Computes the ranks, normal scores, or exponential scores for a vector of observations.

**RANDOM NUMBERS****random\_seed\_get**

Retrieves the current value of the seed used in the IMSL random number generators.

**random\_seed\_set**

Initializes a random seed for use in the IMSL random number generators.

**random\_option**

Selects the uniform (0, 1) multiplicative congruential pseudorandom number generator.

**random\_uniform**

Generates pseudorandom numbers from a uniform (0, 1) distribution.

**random\_normal**

Generates pseudorandom numbers from a standard normal distribution using an inverse CDF method.

**random\_poisson**

Generates pseudorandom numbers from a Poisson distribution.

**random\_gamma**

Generates pseudorandom numbers from a standard gamma distribution.

**random\_beta**

Generates pseudorandom numbers from a beta distribution.

**random\_exponential**

Generates pseudorandom numbers from a standard exponential distribution.

**faure\_next\_point**

Computes a shuffled Faure sequence.

## *CHAPTER 11: PRINTING FUNCTIONS*

---

**PRINT****write\_matrix**

Prints a rectangular matrix (or vector) stored in contiguous memory locations.

**SET****page**

Sets or retrieve the page width or length.

**write\_options**

Sets or retrieve an option for printing a matrix.

## *CHAPTER 12: UTILITIES*

---

**SET OUTPUT FILES****output\_file**

Sets the output file or the error message output file.

**version**

Returns integer information describing the version of the library, license number, operating system, and compiler.

**TIME AND DATE:****ctime**

Returns the number of CPU seconds used.

**date\_to\_days**

Computes the number of days from January 1, 1900, to the given date.

**days\_to\_date**

Gives the date corresponding to the number of days since January 1, 1900.

**ERROR HANDLING****error\_options**

Sets various error handling options.

**error\_code**

Gets the code corresponding to the error message from the last function called.

**CONSTANTS****constant**

Returns the value of various mathematical and physical constants.

**machine (integer)**

Returns integer information describing the computer's arithmetic.

**machine (float)**

Returns information describing the computer's floating-point arithmetic.

## SORTING

### **sort**

Sorts a vector by algebraic value. Optionally, a vector can be sorted by absolute value, and a sort permutation can be returned.

### **sort (integer)**

Sorts an integer vector by algebraic value. Optionally, a vector can be sorted by absolute value, and a sort permutation can be returned.

## COMPUTING VECTOR NORMS

### **vector\_norm**

Computes various norms of a vector or the difference of two vectors.

## LINEAR ALGEBRA SUPPORT

### **mat\_mul\_rect**

Computes the transpose of a matrix, a matrix-vector product, a matrix-matrix product, the bilinear form, or any triple product.

### **mat\_mul\_rect (complex)**

Computes the transpose of a matrix, the conjugate-transpose of a matrix, a matrix-vector product, a matrix-matrix product, the bilinear form, or any triple product.

### **mat\_mul\_rect\_band**

Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices stored in band form.

### **mat\_mul\_rect\_band (complex)**

Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices of complex type and stored in band form.

### **mat\_mul\_rect\_coordinate**

Computes the transpose of a matrix, a matrix-vector product, or a matrix-matrix product, all matrices stored in sparse coordinate form.

### **mat\_mul\_rect\_coordinate (complex)**

Computes the transpose of a matrix, a matrix-vector product or a matrix-matrix product, all matrices stored in sparse coordinate form.

### **mat\_add\_band**

Adds two band matrices, both in band storage mode,  $C \leftarrow \alpha A + \beta B$ .

### **mat\_add\_band (complex)**

Adds two band complex matrices, both in band storage mode,  $C \leftarrow \alpha A + \beta B$ .

### **mat\_add\_coordinate**

Performs element-wise addition of two real matrices stored in coordinate format,  $C \leftarrow \alpha A + \beta B$ .

### **mat\_add\_coordinate (complex)**

Performs element-wise addition on two complex matrices stored in coordinate format,  $C \leftarrow \alpha A + \beta B$ .

### **matrix\_norm**

Computes various norms of a rectangular matrix.

### **matrix\_norm\_band**

Computes various norms of a matrix stored in band storage mode.

### **matrix\_norm\_coordinate**

Computes various norms of a matrix stored in coordinate format.

### **generate\_test\_band**

Generates test matrices of class  $E(n, c)$ .

### **generate\_test\_band (complex)**

Generates test matrices of class  $E_c(n, c)$ .

### **generate\_test\_coordinate**

Generates test matrices of class  $D(n, c)$  and  $E(n, c)$ .

### **generate\_test\_coordinate (complex)**

Generates test matrices of class  $D(n, c)$  and  $E(n, c)$ .

## *Numeric Utilities*

---

### **c\_neg**

Changes the sign of a complex number.

### **c\_add**

Adds two complex numbers.

### **c\_sub**

Subtracts a complex number from a complex number.

### **c\_mul**

Multiplies two complex numbers.

### **c\_div**

Divides a complex number by a complex number.

### **c\_eq**

Tests for equality of two complex numbers.

### **cz\_convert**

Truncates a double precision complex number to a single precision complex number.

### **zc\_convert**

Increases precision of a single precision complex number to a double precision complex number.

### **cf\_convert**

Makes a complex number from an ordered pair.

### **c\_conjg**

Conjunctates a complex number.

### **c\_abs**

Computes a magnitude of a complex number.



**c\_arg**

Computes an angle of a complex number.

**c\_sqrt**

Computes a square root of a complex number.

**c\_cos**

Computes a trigonometric cosine of a complex number.

**c\_sin**

Computes a trigonometric sine of a complex number.

**c\_exp**

Computes an exponential function of a complex number.

**c\_log**

Computes a natural logarithm of a complex number.

**cf\_power**

Computes a complex number raised to a real power.

**cc\_power**

Computes a complex number raised to a complex power.

**fi\_power**

Computes a real number raised to an integral power.

**ii\_power**

Computes an integer raised to an integral power.

## *IMSL C/Stat/Library™*

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### *CHAPTER 1: BASIC STATISTICS*

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**SIMPLE SUMMARY STATISTICS****simple\_statistics**

Computes basic univariate statistics.

**normal\_one\_sample**

Computes statistics for mean and variance inferences using a sample from a normal population.

**normal\_two\_sample**

Computes statistics for mean and variance inferences using samples from two normal populations.

**TABULATE, SORT, RANK****table\_oneway**

Tallies observations into a one-way frequency table.

**table\_twoway**

Tallies observations into a two-way frequency table.

**sort\_data**

Sorts observations by specified keys, with option to tally cases into a multi-way frequency table.

**ranks**

Computes the ranks, normal scores, or exponential scores for a vector of observations.

## *CHAPTER 2: REGRESSION*

---

**MULTIVARIATE LINEAR REGRESSION—MODEL****FITTING****regressors\_for\_glm**

Generates regressors for a general linear model.

**regression**

Fits a multiple linear regression model using least squares.

**MULTIVARIATE LINEAR REGRESSION—  
STATISTICAL INFERENCE AND DIAGNOSTICS****regression\_summary**

Produces summary statistics for a regression model given the information from the fit.

**regression\_prediction**

Computes predicted values, confidence intervals, and diagnostics after fitting a regression model.

**hypothesis\_partial**

Constructs a completely testable hypothesis.

**hypothesis\_scph**

Sums of cross products for a multivariate hypothesis.

**hypothesis\_test**

Tests for the multivariate linear hypothesis.

**VARIABLE SELECTION****regression\_selection**

Selects the best multiple linear regression models.

**regression\_stepwise**

Builds multiple linear regression models using forward selection, backward selection or stepwise selection.

**POLYNOMIAL AND NONLINEAR REGRESSION****poly\_regression**

Performs a polynomial least-squares regression.

**poly\_prediction**

Computes predicted values, confidence intervals, and diagnostics after fitting a polynomial regression model.

**nonlinear\_regression**

Fits a nonlinear regression model.

**nonlinear\_optimization**

Fits a nonlinear regression model using Powell's algorithm.

## ALTERNATIVES TO LEAST SQUARES

### **Lnorm\_regression**

Fits a multiple linear regression model using  $L_p$  criteria other than least squares.

## *CHAPTER 3: CORRELATION AND COVARIANCE*

---

### VARIANCES, COVARIANCES, AND

#### **CORRELATIONS**

##### **covariances**

Computes the sample variance-covariance or correlation matrix.

##### **partial\_covariances**

Computes partial covariances or partial correlations from the covariance or correlation matrix.

##### **pooled\_covariances**

Computes a pooled variance-covariance from the observations.

##### **robust\_covariances**

Computes a robust estimate of a covariance matrix and mean vector.

## *CHAPTER 4: ANALYSIS OF VARIANCE*

---

### ONE-WAY CLASSIFICATION

#### **anova\_oneway**

Analyzes a one-way classification model.

### BALANCED DESIGNS

#### **anova\_factorial**

Analyzes a balanced factorial design with fixed effects.

#### **multiple\_comparisons**

Performs Student-Newman-Keuls multiple comparisons test.

### NESTED DESIGNS

#### **anova\_nested**

Analyzes a completely nested random model with possibly unequal numbers in the subgroups.

### MULTIPLE COMPARISONS TEST

#### **anova\_balanced**

Analyzes a balanced complete experimental design for a fixed, random, or mixed model.

## *CHAPTER 5: CATEGORICAL AND DISCRETE DATA ANALYSIS*

---

### STATISTICS IN THE TWO-WAY CONTINGENCY

#### **TABLE**

##### **contingency\_table**

Performs a chi-squared analysis of a two-way contingency table.

##### **exact\_enumeration**

Computes exact probabilities in a two-way contingency table, using the total enumeration method.

##### **exact\_network**

Computes exact probabilities in a two-way contingency table using the network algorithm.

### GENERALIZED CATEGORICAL MODELS

#### **categorical\_glm**

Analyzes categorical data using logistic, Probit, Poisson, and other generalized linear models.

## *CHAPTER 6: NONPARAMETRIC STATISTICS*

---

### ONE SAMPLE TESTS—NONPARAMETRIC

#### **STATISTICS**

##### **sign\_test**

Performs a sign test.

##### **wilcoxon\_sign\_rank**

Performs a Wilcoxon rank sum test.

##### **noether\_cyclical\_trend**

Performs the Noether's test for cyclical trend.

##### **cox\_stuart\_trends\_test**

Performs the Cox and Stuart' sign test for trends in location and dispersion.

##### **tie\_statistics**

Computes tie statistics for a sample of observations.

### TWO OR MORE SAMPLES

#### **wilcoxon\_rank\_sum**

Performs a Wilcoxon rank sum test.

#### **kruskal\_wallis\_test**

Performs a Kruskal-Wallis's test for identical population medians.

#### **friedmans\_test**

Performs Friedman's test for a randomized complete block design.

#### **cochran\_q\_test**

Performs Cochran's  $Q$  test for related observations.

#### **k\_trends\_test**

Performs k-sample trends test against ordered alternatives.

## CHAPTER 7: TESTS OF GOODNESS OF FIT

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### GENERAL GOODNESS-OF-FIT-TESTS

#### **chi\_squared\_test**

Performs a chi-squared goodness-of-fit test.

#### **normality\_test**

Performs a test for normality.

#### **kolmogorov\_one**

Performs a Kolmogorov-Smirnov's one-sample test for continuous distributions.

#### **kolmogorov\_two**

Performs a Kolmogorov-Smirnov's two-sample test

#### **multivar\_normality\_test**

Computes Mardia's multivariate measures of skewness and kurtosis and tests for multivariate normality.

### TESTS FOR RANDOMNESS

#### **randomness\_test**

Performs a test for randomness.

## CHAPTER 8: TIME SERIES AND FORECASTING

---

### ARIMA MODELS

#### **arma**

Computes least-square estimates of parameters for an ARMA model.

#### **arma\_forecast**

Computes forecasts and their associated probability limits for an ARMA model.

#### **difference**

Differences a seasonal or nonseasonal time series.

#### **box\_cox\_transform**

Performs a Box-Cox transformation.

#### **autocorrelation**

Computes the sample autocorrelation function of a stationary time series.

#### **partial\_autocorrelation**

Computes the sample partial autocorrelation function of a stationary time series.

#### **lack\_of\_fit**

Performs lack-of-fit test for an univariate time series or transfer function given the appropriate correlation function.

#### **garch**

Computes estimates of the parameters of a GARCH( $p, q$ ) model.

#### **kalman**

Performs Kalman filtering and evaluates the likelihood function for the state-space model.

## CHAPTER 9: MULTIVARIATE ANALYSIS

---

### CLUSTER ANALYSIS

#### **cluster\_k\_means**

Performs a  $K$ -means (centroid) cluster analysis.

### PRINCIPAL COMPONENTS

#### **principal\_components**

Computes principal components.

### FACTOR ANALYSIS

#### **factor\_analysis**

Extracts initial factor-loading estimates in factor analysis.

### DISCRIMINANT ANALYSIS

#### **discriminant\_analysis**

Performs discriminant function analysis.

## CHAPTER 10: SURVIVAL ANALYSIS

---

### GENERALIZED LINEAR MODEL

#### **survival\_glm**

Analyzes survival data using a generalized linear model.

### PARAMETRIC ESTIMATES

#### **survival\_estimates**

Estimates using various parametric models.

## CHAPTER 11: PROBABILITY AND DISTRIBUTION FUNCTIONS

---

### DISCRETE RANDOM VARIABLES

#### **binomial\_cdf**

Evaluates the binomial distribution function.

#### **binomial\_pdf**

Evaluates the binomial probability function.

#### **hypergeometric\_cdf**

Evaluates the hypergeometric distribution function.

#### **poisson\_cdf**

Evaluates the Poisson distribution function.

### CONTINUOUS RANDOM VARIABLES

#### **beta\_cdf**

Evaluates the beta probability distribution function.

#### **beta\_inverse\_cdf**

Evaluates the inverse of the beta distribution function.

#### **bivariate\_normal\_cdf**

Evaluates the bivariate normal distribution function.

**bivariate\_normal\_cdf**

Evaluates the bivariate normal distribution function.

**bivariate\_normal\_cdf**

Evaluates the bivariate normal distribution function.

**chi\_squared\_cdf**

Evaluates the chi-squared distribution function.

**chi\_squared\_inverse\_cdf**

Evaluates the inverse of the chi-squared distribution function.

**non\_central\_chi\_sq**

Evaluates the noncentral chi-squared distribution function.

**non\_central\_chi\_sq\_inv**

Evaluates the inverse of the noncentral chi-squared function.

**F\_cdf**

Evaluates the  $F$  distribution function.

**F\_inverse\_cdf**

Evaluates the inverse of the  $F$  distribution function.

**gamma\_cdf**

Evaluates the gamma distribution function.

**normal\_cdf**

Evaluates the standard normal (Gaussian) distribution function.

**normal\_inverse\_cdf**

Evaluates the inverse of the standard normal (Gaussian) distribution function.

**t\_cdf**

Evaluates the Student's  $t$  distribution function.

**t\_inverse\_cdf**

Evaluates the inverse of the Student's  $t$  distribution function.

**non\_central\_t\_cdf**

Evaluates the noncentral Student's  $t$  distribution function.

**non\_central\_t\_inv\_cdf**

Evaluates the inverse of the noncentral Student's  $t$  distribution function.

## CHAPTER 12: RANDOM NUMBER GENERATION

---

**UNIVARIATE DISCRETE DISTRIBUTIONS****random\_binomial**

Generates pseudorandom binomial numbers.

**random\_geometric**

Generates pseudorandom numbers from a geometric distribution.

**random\_hypergeometric**

Generates pseudorandom numbers from a hypergeometric distribution.

**random\_logarithmic**

Generates pseudorandom numbers from a logarithmic distribution.

**random\_neg\_binomial**

Generates pseudorandom numbers from a negative binomial distribution.

**random\_poisson**

Generates pseudorandom numbers from a Poisson distribution.

**random\_uniform\_discrete**

Generates pseudorandom numbers from a discrete uniform distribution.

**random\_general\_discrete**

Generates pseudorandom numbers from a general discrete distribution using an alias method or optionally a table lookup method.

**discrete\_table\_setup**

Sets up a table to generate pseudorandom numbers from a general discrete distribution.

**UNIVARIATE CONTINUOUS DISTRIBUTIONS****random\_beta**

Generates pseudorandom numbers from a beta distribution.

**random\_cauchy**

Generates pseudorandom numbers from a Cauchy distribution.

**random\_chi\_squared**

Generates pseudorandom numbers from a chi-squared distribution.

**random\_exponential**

Generates pseudorandom numbers from a standard exponential distribution.

**random\_exponential\_mix**

Generates pseudorandom mixed numbers from a standard exponential distribution.

**random\_gamma**

Generates pseudorandom numbers from a standard gamma distribution.

**random\_lognormal**

Generates pseudorandom numbers from a lognormal distribution.

**random\_normal**

Generates pseudorandom numbers from a standard normal distribution using an inverse CDF method.

**random\_stable**

Sets up a table to generate pseudorandom numbers from a general discrete distribution.

**random\_student\_t**

Generates pseudorandom Student's  $t$ .

**random\_triangular**

Generates pseudorandom numbers from a triangular distribution.

**random\_uniform**

Generates pseudorandom numbers from a uniform (0, 1) distribution.

**random\_von\_mises**

Generates pseudorandom numbers from a von Mises distribution.

**random\_weibull**

Generates pseudorandom numbers from a Weibull distribution.

**random\_general\_continuous**

Generates pseudorandom numbers from a general continuous distribution.

**continuous\_table\_setup**

Sets up a table to generate pseudorandom numbers from a general continuous distribution.

**MULTIVARIATE CONTINUOUS DISTRIBUTIONS****random\_normal\_multivariate**

Generates pseudorandom numbers from a multivariate normal distribution.

**random\_orthogonal\_matrix**

Generates a pseudorandom orthogonal matrix or a correlation matrix.

**random\_mvar\_from\_data**

Generates pseudorandom numbers from a multivariate distribution determined from a given sample.

**random\_multinomial**

Generates pseudorandom numbers from a multinomial distribution.

**random\_sphere**

Generates pseudorandom points on a unit circle or  $\kappa$ -dimensional sphere.

**random\_table\_twoway**

Generates a pseudorandom two-way table.

**ORDER STATISTICS****random\_order\_normal**

Generates pseudorandom order statistics from a standard normal distribution.

**random\_order\_uniform**

Generates pseudorandom order statistics from a uniform (0, 1) distribution.

**STOCHASTIC PROCESSES****random\_arma**

Generates pseudorandom ARMA process numbers.

**random\_npp**

Generates pseudorandom numbers from a nonhomogeneous Poisson process.

**SAMPLES AND PERMUTATIONS****random\_permutation**

Generates a pseudorandom permutation.

**random\_sample\_indices**

Generates a simple pseudorandom sample of indices.

**random\_sample**

Generates a simple pseudorandom sample from a finite population.

**UTILITY FUNCTIONS****random\_option**

Selects the uniform (0, 1) multiplicative congruential pseudorandom number generator.

**random\_option\_get**

Retrieves the uniform (0, 1) multiplicative congruential pseudorandom number generator.

**random\_seed\_get**

Retrieves the current value of the seed used in the IMSL random number generators.

**random\_substream\_seed\_get**

Retrieves a seed for the congruential generators that do not do shuffling that will generate random numbers beginning 100,000 numbers farther along.

**random\_seed\_set**

Initializes a random seed for use in the IMSL random number generators.

**random\_table\_set**

Sets the current table used in the shuffled generator.

**random\_table\_get**

Retrieves the current table used in the shuffled generator.

**random\_GFSR\_table\_set**

Sets the current table used in the GFSR generator.

**random\_GFSR\_table\_get**

Retrieves the current table used in the GFSR generator.

**LOW-DISCREPANCY SEQUENCE****faure\_next\_point**

Computes a shuffled Faure sequence

**CHAPTER 13: PRINTING FUNCTIONS**

---

**PRINT****write\_matrix**

Prints a rectangular matrix (or vector) stored in contiguous memory locations.

## **SET**

### **page**

Sets or retrieves the page width or length.

### **write\_options**

Sets or retrieves an option for printing a matrix.

## **CHAPTER 14: UTILITIES**

---

### **SET OUTPUT FILES**

#### **output\_file**

Sets the output file or the error message output file.

#### **version**

Returns integer information describing the version of the library, license number, operating system, and compiler.

### **ERROR HANDLING**

#### **error\_options**

Sets various error handling options.

#### **error\_code**

Returns the code corresponding to the error message from the last function called.

### **CONSTANTS**

#### **machine (integer)**

Returns integer information describing the computer's arithmetic.

#### **machine (float)**

Returns information describing the computer's floating-point arithmetic.

#### **data\_sets**

Retrieves a commonly analyzed data set.

### **MATHEMATICAL SUPPORT**

#### **mat\_mul\_rect**

Computes the transpose of a matrix, a matrix-vector product, a matrix-matrix product, a bilinear form, or any triple product.

#### **permute\_vector**

Rearranges the elements of a vector as specified by a permutation.

#### **permute\_matrix**

Permutes the rows or columns of a matrix.

#### **binomial\_coefficient**

Evaluates the binomial coefficient.

#### **beta**

Evaluates the complete beta function.

#### **beta\_incomplete**

Evaluates the real incomplete beta function.

#### **og\_beta**

Evaluates the log of the real beta function.

#### **gamma**

Evaluates the real gamma functions.

#### **gamma\_incomplete**

Evaluates the incomplete gamma function.

#### **log\_gamma**

Evaluates the logarithm of the absolute value of the gamma function.

#### **ctime**

Returns the number of CPU seconds used.

## IMSL FORTRAN 90 MP LIBRARY

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The IMSL Fortran 90 MP Library ("F90MP") is used by technical professionals for business, engineering, finance, research and education applications worldwide. Users can leverage the high performance technology of vector processors, shared memory parallelism and/or distributed memory parallelism and at the same time continue to obtain reliable results from the mathematical and statistical functionality within this library.

F90MP provides Fortran 90 coded, not translated, subroutines. Our implementation complies with the ANSI and ISO standards. The incorporation of array syntax provides performance gains with optimized compilers. The object-oriented interface provides easy access to the underlying algorithms.

F90MP also provides backward compatibility for developers who have used our FORTRAN 77 functions; all of the FORTRAN 77 function definitions are included in the IMSL Fortran 90 MP Library.

## JNL - A NUMERICAL LIBRARY FOR JAVA™

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JNL is a 100% Pure Java numerical library for the Java environment. The library extends core Java numerics and allows developers to seamlessly integrate advanced mathematical functions into their Java applications.

JNL is an object-oriented implementation of several important classes of mathematical functions drawn from the IMSL algorithm repository. Visual Numerics has taken individual algorithms and reimplemented them as object-oriented, Java methods. JNL is designed with extensibility in mind; new classes may be derived from existing ones to add functionality to satisfy particular requirements.

Because JNL is a 100% Pure Java class library, it can be deployed on any platform that supports Java. A JNL-based application will work seamlessly on a PC, a Macintosh, a UNIX workstation or any other Java-enabled platform.

JNL can be used to write client-side applets, server-side applications or even non-networked desktop applications. JNL applets perform all processing on the Java client, whether it is a thin client, such as a network computer, a PC or workstation equipped with a Java Virtual Machine. Client-side processing reduces the number of "round trips" to a networked server, which in turn minimizes network traffic and system latency. JNL is Visual Numerics' contribution to the worldwide Java development community, and is available free of charge via our website.

# C Numerical Library Version 5.0

With over  
**75** new  
functions!

- 50 new functions in the area of finance and bonds, intended to help brokerage firms or insurance companies perform financial modeling to analyze various risk factors associated with their business. We've also included routines for calculating depreciation of assets, internal rates of return, bond amortization, and net present values.
- A time series routine useful in navigation, surveying, vehicle tracking (aircraft, spacecraft, missiles), geology, oceanography, fluid dynamics, steel/paper/power industries, and demographic estimation.
- Routines to compute low discrepancy series of random points using a generalized Faure sequence.
- An algorithm for efficient multi-dimensional quadrature. Very high-dimension quadrature arises in some financial optimization applications. Such integrals are used in evaluating collateralized mortgage obligations (CMOs). Valuing a 30-year (360 month) CMO requires that an integral over a 360 dimensions box be evaluated.
- More than twenty new random number routines, including Generalized Feedback Shift Register (GFSR) generator support.

## Platform & System Requirements

<b>Platform</b>	<b>Operating System</b>	<b>Compiler</b>
Silicon Graphics 64 bit	IRIX 6.5	MIPSpro C, Version 7.3.1.1m
Compaq Alpha	TRU64 UNIX, Version 5.1-732	Compaq C V6.3-025
Fujitsu 300 / 500 / 700 / SX	VPP5000UU UPX/V V L	UXP/V C V20L20 Driver L99121
HP PA/RISC 1.1 32 bit	HP-UX Release 11.0	HP92453-01 A.11.01.20 HP C Compiler
HP PA/RISC 2.0 64 bit	HP-UX Release 11.0	HP92453-01 A.11.01.20 HP C Compiler
Intel Based systems	Red Hat Linux 6.1	egcs-2.91.66
Intel Based systems	Windows 98/NT/2000	Visual C++ 6.0
IBM RS/6000 32-bit	AIX, Version 4.3.3	C and C++ Compilers Version 3.6.6.0 & C for AIX Compiler Version 5.0.0.0
IBM RS/6000 64-bit	AIX, Version 4.3.3	C and C++ Compilers Version 3.6.6.0 & C for AIX Compiler Version 5.0.0.0
Sun SPARC 32-bit	Sun Solaris, Version 7.0	Workshop Compiler C 5.1
Sun SPARC 64-bit	Sun Solaris, Version 7.0	Workshop Compiler C 5.1

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