

# Hadron-Quark phase transition in high-mass neutron stars

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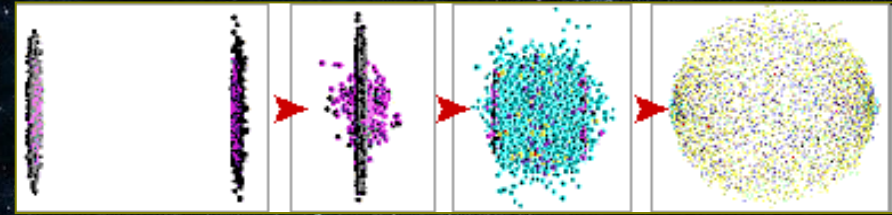
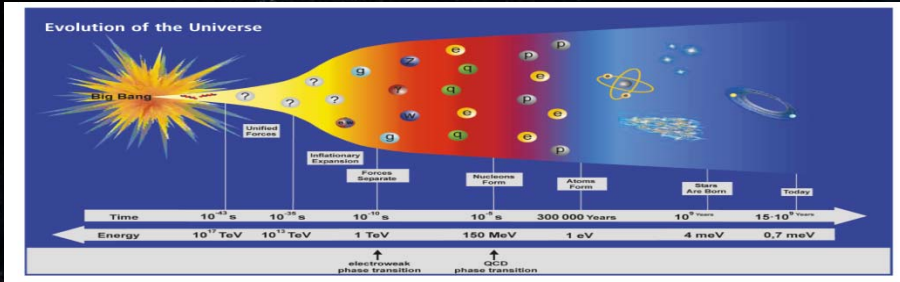


## IV IWARA 2013

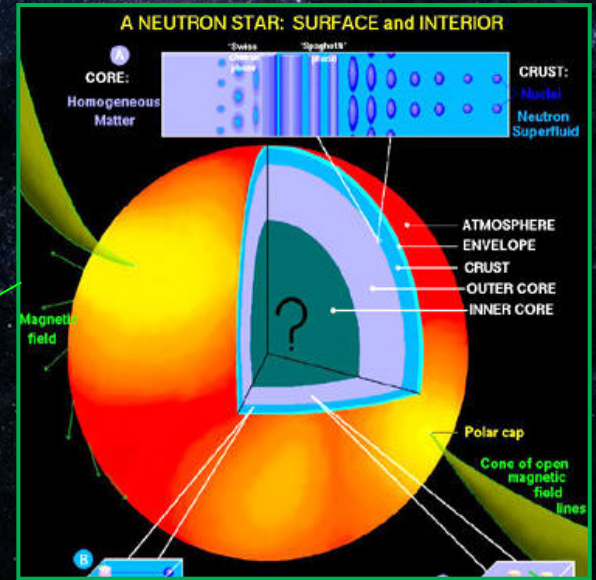
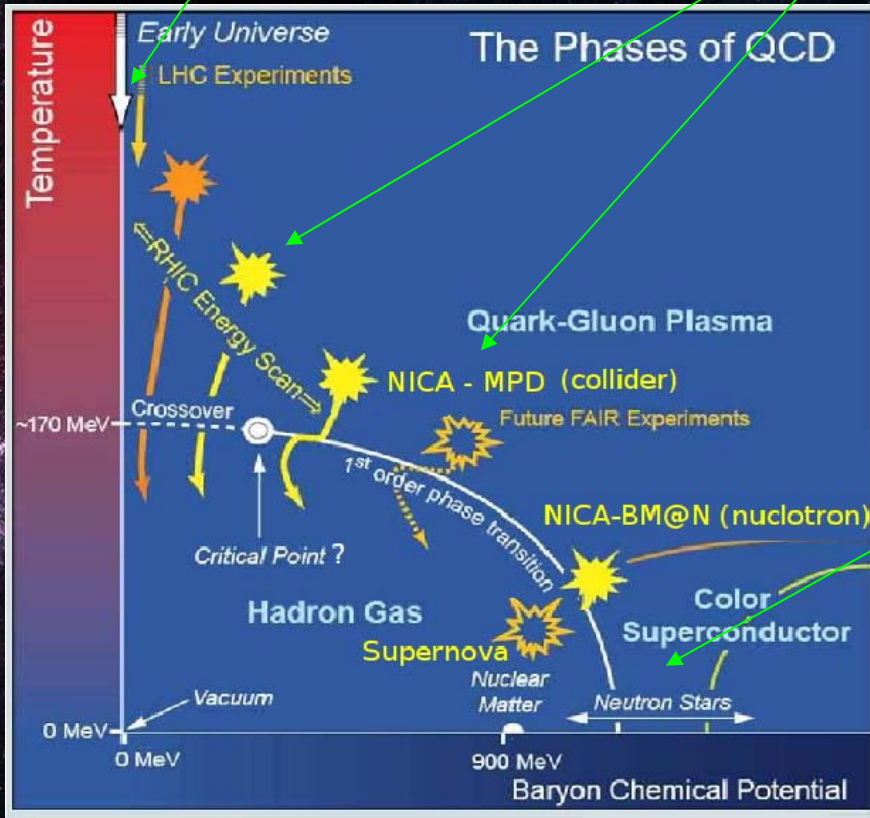
September 30th to October 3rd; Rio de Janeiro, Brazil

# Motivation

## Cosmology

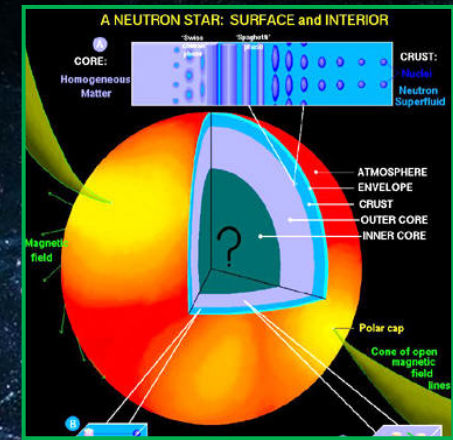
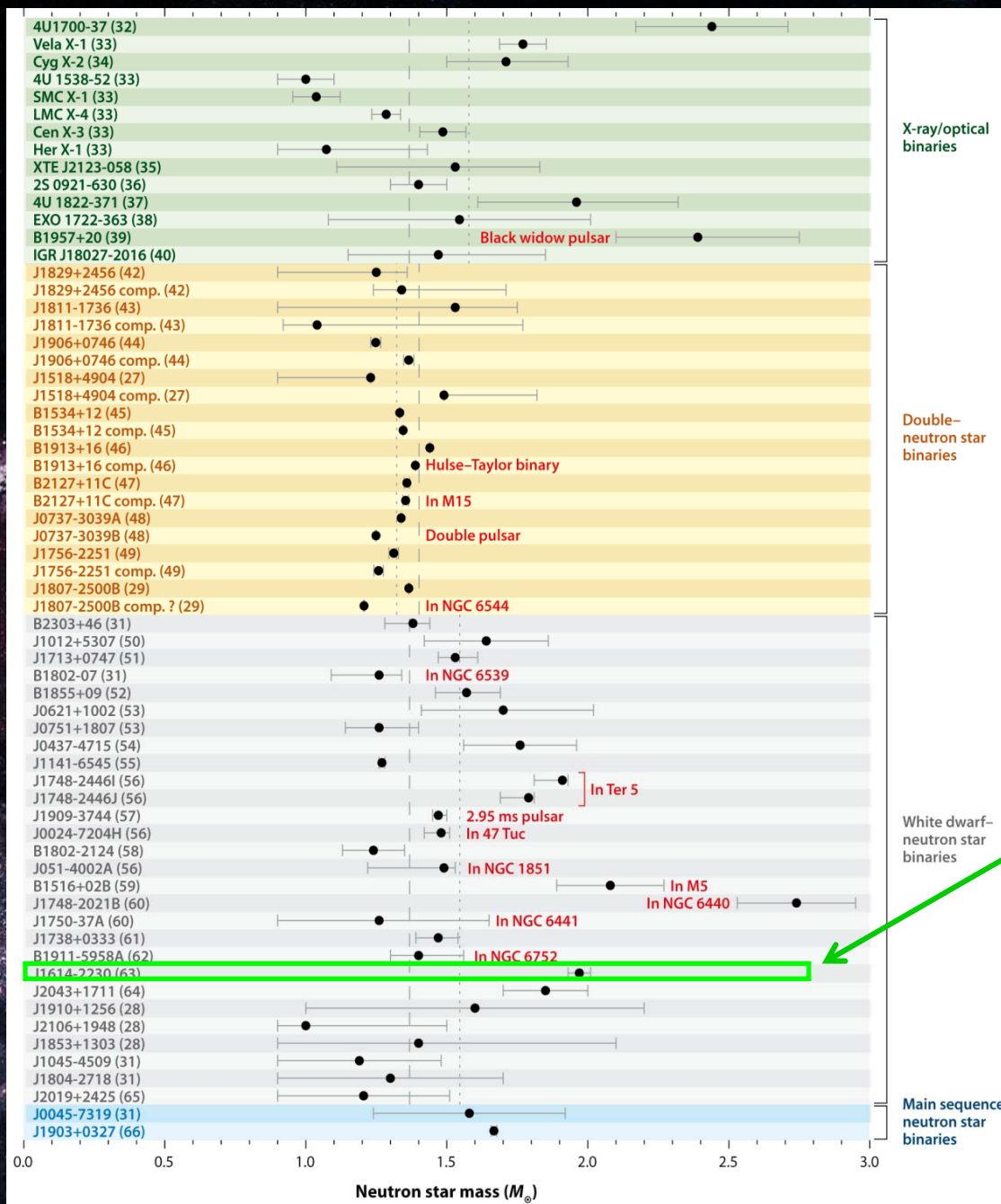


Heavy ion and  $p^+p^+$  collisions (RHIC, LHC, FAIR, NICA ...)



Compact stars astrophysics

QCD Phase Diagram?



PSR J1614 – 2230  
 ( $M = 1.97 \pm 0.04 M_{\text{sun}}$ )

Demorest et al.  
 Nature 467, 1081 (2010).

# Motivation

- Recent high precision determination of two high mass Neutron Stars (NS) J1614-2230 ( $1.97 \pm 0.04 M_{\text{Sun}}$ ) [1] and J0348+0432 ( $2.01 \pm 0.04 M_{\text{Sun}}$ ) [2].

[1] P. B. Demorest et al, Nature 467, 1081 (2010).

[2] L. Antoniadis et al, Science 340, 6131 (2013).

- What are the fundamental building blocks in the core of such stars?
- Does quark deconfinement occur?

How could we modelate matter under such conditions?

- We have analyzed the global structure and composition of massive NSs in the framework of a non-local 3-flavor NJL model (**n3NJL**) for quark matter and a non-linear relativistic model for hadronic matter [3,4].

[3] M. Orsaria, H. Rodrigues, F. Weber, G. A. Contrera, Phys. Rev. D 87, 023001 (2013).

[4] M. Orsaria, H. Rodrigues, F. Weber, G. A. Contrera, arXiv:1308.1657 [nucl-th].

# Quark Phase: Local vs. Non-local NJL models

Local NJL	Non-local NJL model
<ul style="list-style-type: none"><li>• Lack of confinement</li></ul>	<ul style="list-style-type: none"><li>• Confinement with a proper choice of the non-local regulator and model parameters [1]</li></ul>
<ul style="list-style-type: none"><li>• Quark-quark scalar-isoscalar and pseudoscalar-isovectorial local interaction</li></ul>	<ul style="list-style-type: none"><li>• Quark-quark interaction through phenomenologically effective quark propagator</li></ul>
<ul style="list-style-type: none"><li>• Non-renormalizable. Ultra-violet (UV) cutoff <math>\Lambda</math> is needed</li></ul>	<ul style="list-style-type: none"><li>• UV divergences are fixed [2] Model dependent form factor <math>g(p)</math></li></ul>
<ul style="list-style-type: none"><li>• Dynamical quark masses are momentum independent</li></ul>	<ul style="list-style-type: none"><li>• Dynamical quark masses are momentum dependent as also found in lattice calculations of QCD [3]</li></ul>
<ul style="list-style-type: none"><li>• Divergences in the meson loop integrals. Extra cutoffs are needed.</li></ul>	<ul style="list-style-type: none"><li>• The momentum dependent regulator makes the theory finite to all orders in the <math>1/N_c</math> expansion [4]</li></ul>
<ul style="list-style-type: none"><li>• The cutoff <math>\Lambda</math> is turned off at high momenta, limiting the applicability of the model at high densities</li></ul>	<ul style="list-style-type: none"><li>• The form factor provides a natural cutoff that falls off at high momenta</li></ul>

[1] Bowler & Birse, Nucl. Phys. A 582, 655 (1995); Plant & Birse, Nucl. Phys. A 628, 607 (1998);

[2] G. Ripka, Quarks bound by chiral fields (Oxford University Press, Oxford, 1997);

[3] Parappilly et al., Phys. Rev. D 73, 054504 (2006);

[4] D. Blaschke et al., Phys. Rev. C 53, 2394 (1996).

# Quark Phase: n3NJL

Euclidean effective action including vector interaction

$$S_E = \int d^4x \left\{ \bar{\psi}(x) [-i\not{\partial} + \hat{m}] \psi(x) - \frac{G_S}{2} [j_a^S(x) j_a^S(x) + j_a^P(x) j_a^P(x)] - \frac{H}{4} T_{abc} [j_a^S(x) j_b^S(x) j_c^S(x) - 3 j_a^S(x) j_b^P(x) j_c^P(x)] - \frac{G_V}{2} j_V^\mu(x) j_V^\mu(x) \right\}$$

$$j_a^S(x) = \int d^4z \tilde{g}(z) \bar{\psi} \left( x + \frac{z}{2} \right) \lambda_a \psi \left( x - \frac{z}{2} \right) ,$$
$$j_a^P(x) = \int d^4z \tilde{g}(z) \bar{\psi} \left( x + \frac{z}{2} \right) i \gamma_5 \lambda_a \psi \left( x - \frac{z}{2} \right)$$
$$j_V^\mu(x) = \int d^4z \tilde{g}(z) \bar{\psi} \left( x + \frac{z}{2} \right) \gamma^\mu \psi \left( x - \frac{z}{2} \right) ,$$

Form factor responsible for the non-local interaction

After the standard bosonization of the Euclidean action...

$$\Omega^{NL}(M_f, 0, \mu_f) = -\frac{N_c}{\pi^3} \sum_{f=u,d,s} \int_0^\infty dp_0 \int_0^\infty dp \ln \left\{ [\widehat{\omega}_f^2 + M_f^2(\omega_f^2)] \frac{1}{\omega_f^2 + m_f^2} \right\} \\ - \frac{N_c}{\pi^2} \sum_{f=u,d,s} \int_0^{\sqrt{\mu_f^2 - m_f^2}} dp p^2 [(\mu_f - E_f)\theta(\mu_f - m_f)] - \frac{1}{2} \left[ \sum_{f=u,d,s} (\bar{\sigma}_f \bar{S}_f + \frac{G_S}{2} \bar{S}_f^2) + \frac{H}{2} \bar{S}_u \bar{S}_d \bar{S}_s \right] - \sum_{f=u,d,s} \frac{\varpi_f^2}{4G_V}$$

$$N_c = 3, E_f = \sqrt{p^2 + m_f^2}, \text{ and } \omega_f^2 = (p_0 + i\mu_f)^2 + p^2$$

$$M_f(\omega_f^2) = m_f + \bar{\sigma}_f g(\omega_f^2)$$

$$\mu_f \rightarrow \widehat{\mu}_f = \mu_f - g(\omega_f^2)\varpi_f$$

$$g(\omega_f^2) = \exp(-\omega_f^2/\Lambda^2)$$

$$\omega_f^2 \rightarrow \widehat{\omega}_f^2 = (p_0 + i\widehat{\mu}_f)^2 + p^2$$

$$\bar{S}_f = -16 N_c \int_0^\infty dp_0 \int_0^\infty \frac{dp}{(2\pi)^3} g(\omega_f^2) \frac{M_f(\omega_f^2)}{\widehat{\omega}_f^2 + M_f^2(\omega_f^2)}$$

$$\frac{\partial \Omega^{NL}}{\partial \bar{\sigma}_f} = 0, \quad \frac{\partial \Omega^{NL}}{\partial \varpi_f} = 0$$

# Hadronic Phase

- Non-linear Relativistic Mean Field approximation

$$\mathcal{L} = \mathcal{L}_H + \mathcal{L}_\ell$$

$$\mathcal{L}_\ell = \sum_{\lambda=e^-, \mu^-} \bar{\psi}_\lambda (i\gamma_\mu \partial^\mu - m_\lambda) \psi_\lambda$$

$$\begin{aligned} \mathcal{L}_H = & \sum_{B=n,p,\Lambda,\Sigma,\Xi} \bar{\psi}_B [\gamma_\mu (i\partial^\mu - g_\omega \omega^\mu - g_\rho \vec{\rho}_\mu) - (m_N - g_\sigma \sigma)] \psi_B \\ & + \frac{1}{2} (\partial_\mu \sigma \partial^\mu \sigma - m_\sigma^2 \sigma^2) - \frac{1}{3} b_\sigma m_N (g_\sigma \sigma)^3 - \frac{1}{4} c_\sigma (g_\sigma \sigma)^4 \\ & - \frac{1}{4} \omega_{\mu\nu} \omega^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{1}{2} m_\rho^2 \vec{\rho}_\mu \cdot \vec{\rho}^\mu - \frac{1}{4} \vec{\rho}_{\mu\nu} \vec{\rho}^{\mu\nu} \end{aligned}$$

- Full baryon octet:  $p, n, \Lambda, \Sigma^+, \Sigma^0, \Xi^0, \Xi^-, \Xi^0$
- Mesons:  $\sigma, \omega, \rho$
- Leptons:  $e^-, \mu^-$



# Hadronic Phase

Coupling constants	Parametrizations		
	GM1	GM3	NL3
$g_\sigma$	8.910	8.175	10.217
$g_\omega$	10.610	8.172	12.868
$g_\rho$	8.196	8.259	8.948
$b_\sigma$	0.002947	0.008659	0.002055
$c_\sigma$	-0.001070	-0.002421	-0.002651

Properties	Parametrizations		
	GM1	GM3	NL3
$\rho_0$ (fm <sup>-3</sup> )	0.153	0.153	0.148
$E/N$ (MeV)	-16.3	-16.3	-16.3
$K$ (MeV)	300	240	272
$m^*/m_N$	0.78	0.70	0.60
$a_{\text{sy}}$ (MeV)	32.5	32.5	37.4

- [1] N. K. Glendenning, S. A. Moszkowski, Phys. Rev. Lett, 67, 2414 (1991).  
 [2] G. A. Lalazissis, J. Konig, P. Ring, Phys. Rev. C 55, 540 (1997).

# Mixed Quark-Hadron Phase: Gibbs conditions

$$P^H(\mu_b^H, \mu_e^H, \{\phi\}) = P^q(\mu_b^q, \mu_e^q, \{\psi\})$$

$$\mu_b^H = \mu_b^q$$

$$\mu_e^H = \mu_e^q$$

$$n_b = (1 - \chi)n_b^H + \chi n_b^q$$

$$\mu_b = 1/3 \sum_f \mu_f$$

$$\varepsilon = (1 - \chi)\varepsilon^H + \chi\varepsilon^q$$

$$\mu_f = \mu_b - Q\mu_e$$

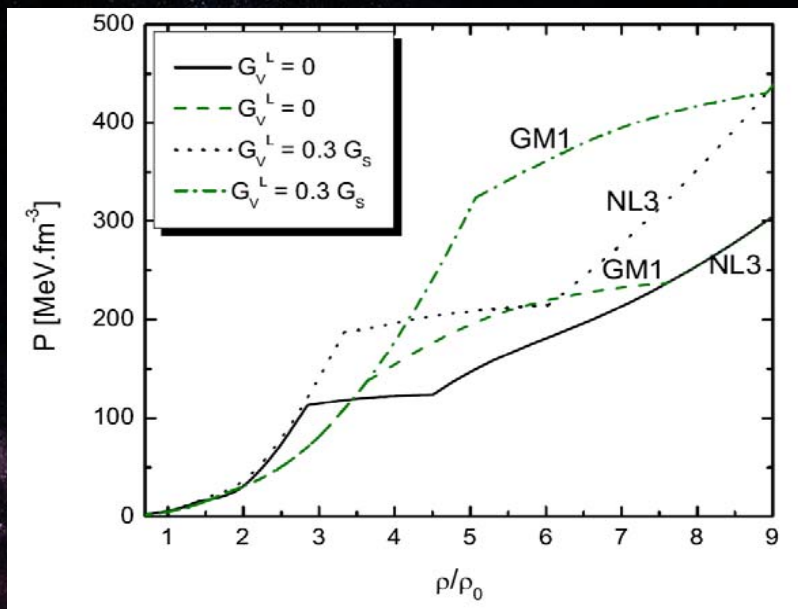
$$\chi = \frac{n^q}{(n^q + n^H)}$$

$$Q = \text{diag}(2/3, -1/3, -1/3)$$

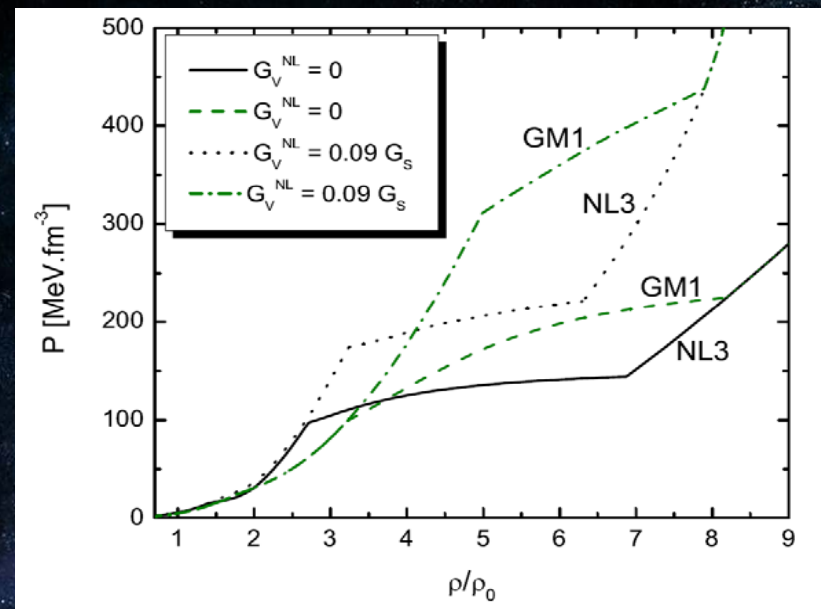
Global electric  
charge neutrality

$$(1 - \chi) \sum_{i=B,l} q_i^H n_i^H + \chi \sum_{i=q,l} q_i^q n_i^q = 0$$

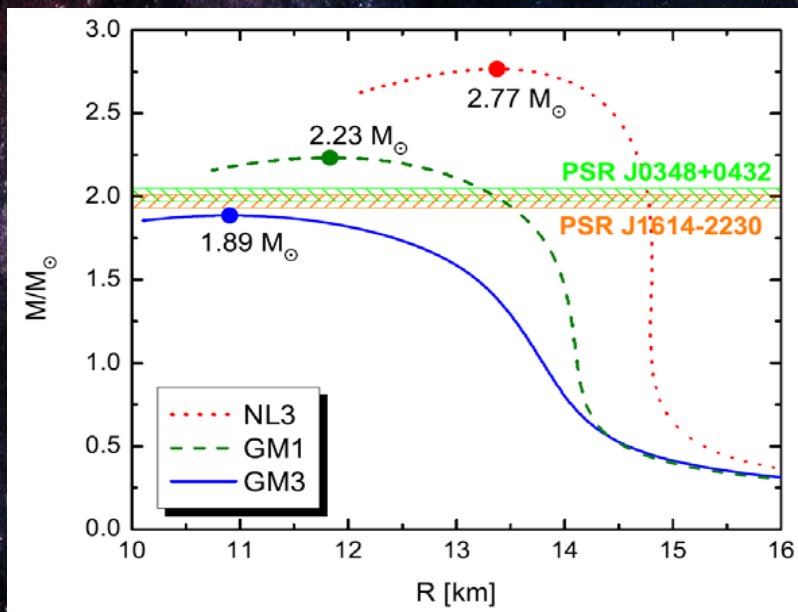
## EoS for Local NJL model



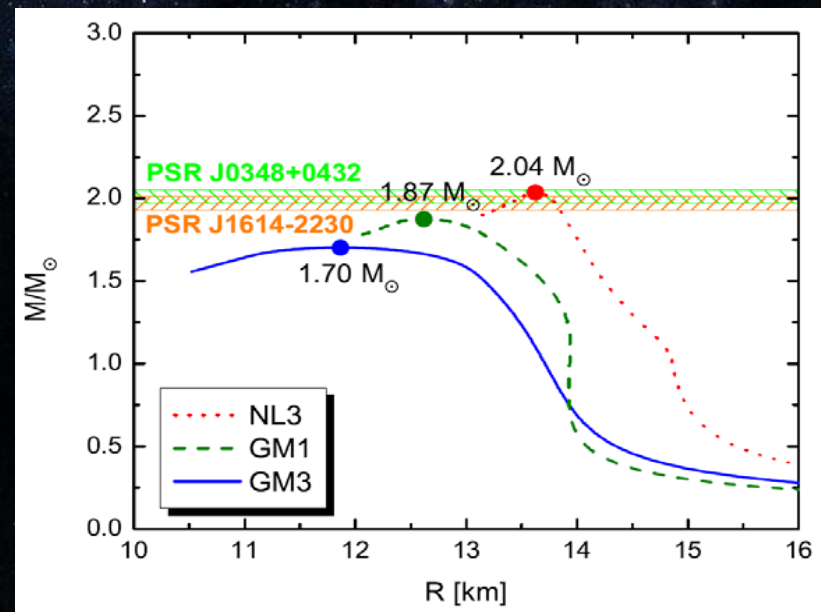
## EoS for non-local NJL model



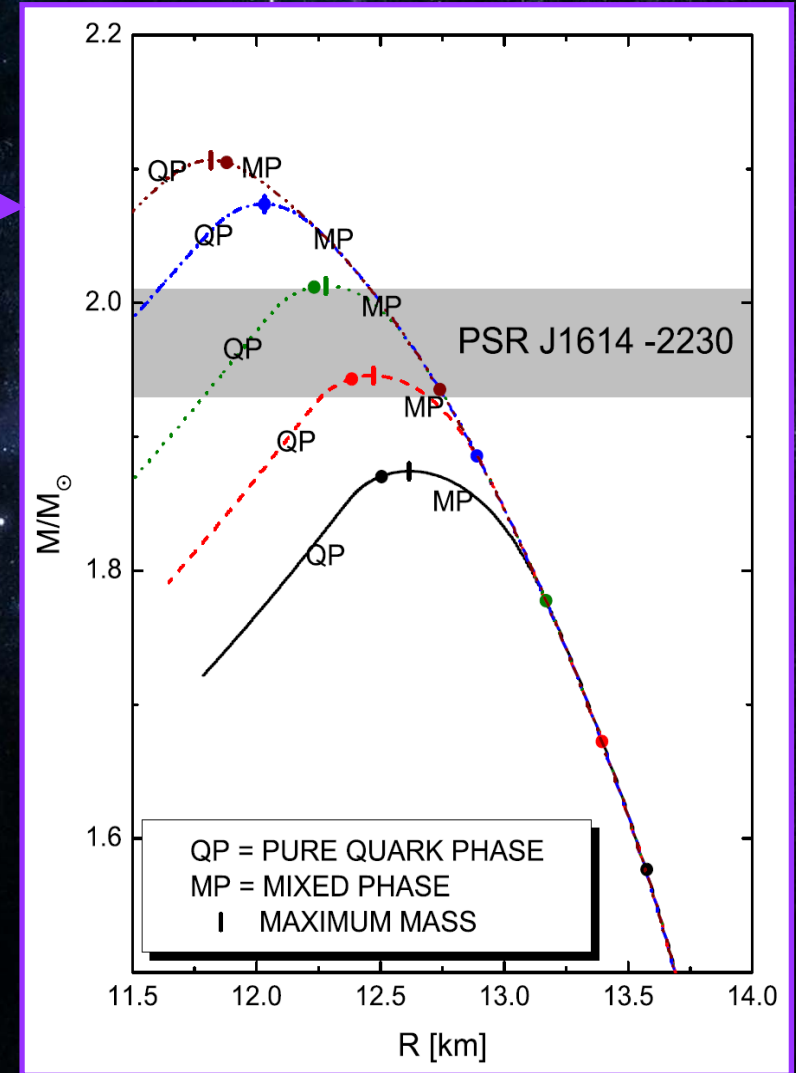
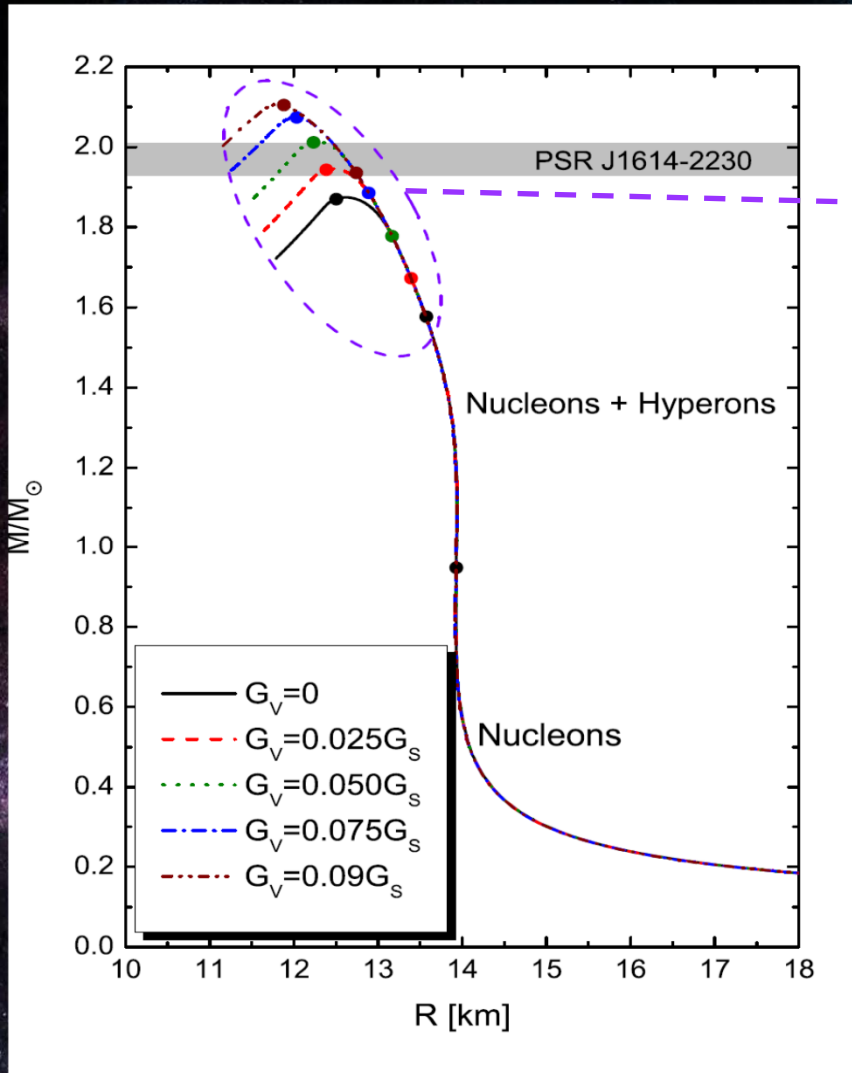
## pure Hadronic stars



## stars with a mixed phase (hadrons+quarks)



# Vector interactions and Mass - Radius relation



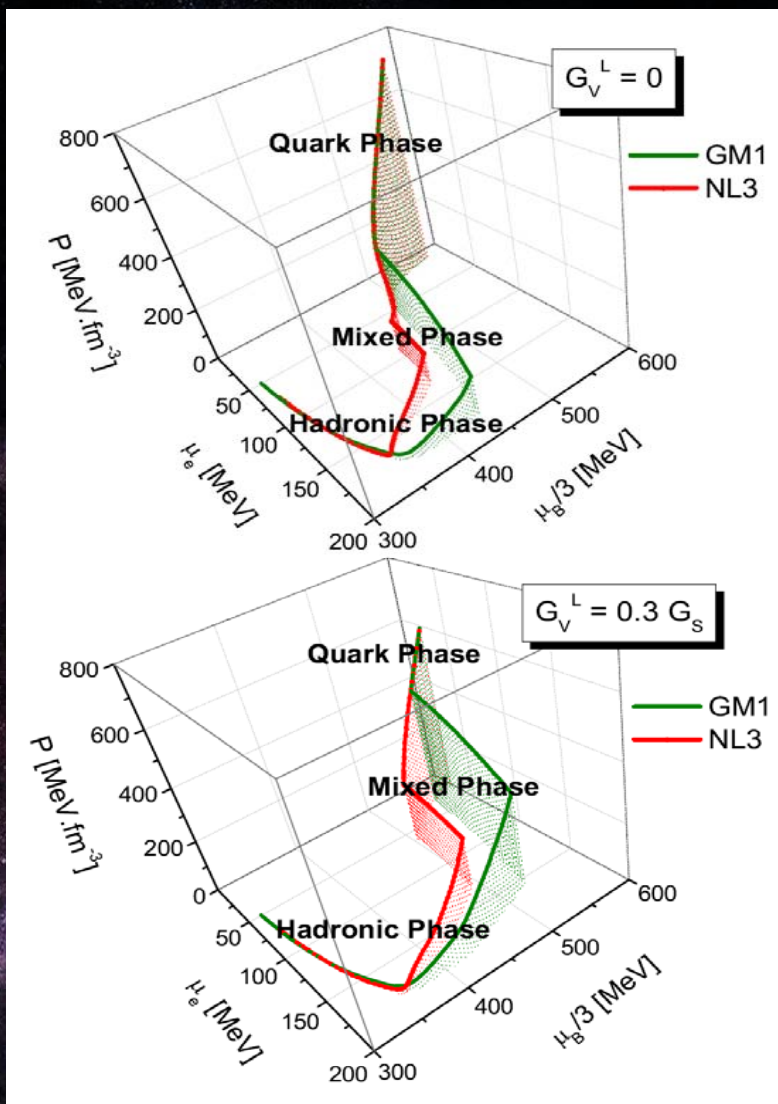


Figure 3. (Color online) Pressure as a function of neutron ( $\mu^n = \mu_B/3$ ) and electron ( $\mu^e$ ) chemical potential for the local NJL model, l3NJL, hadronic parametrizations GM1 and NL3, and vector repulsions  $G_V^L/G_S = 0$  and  $G_V^L/G_S = 0.3$ .

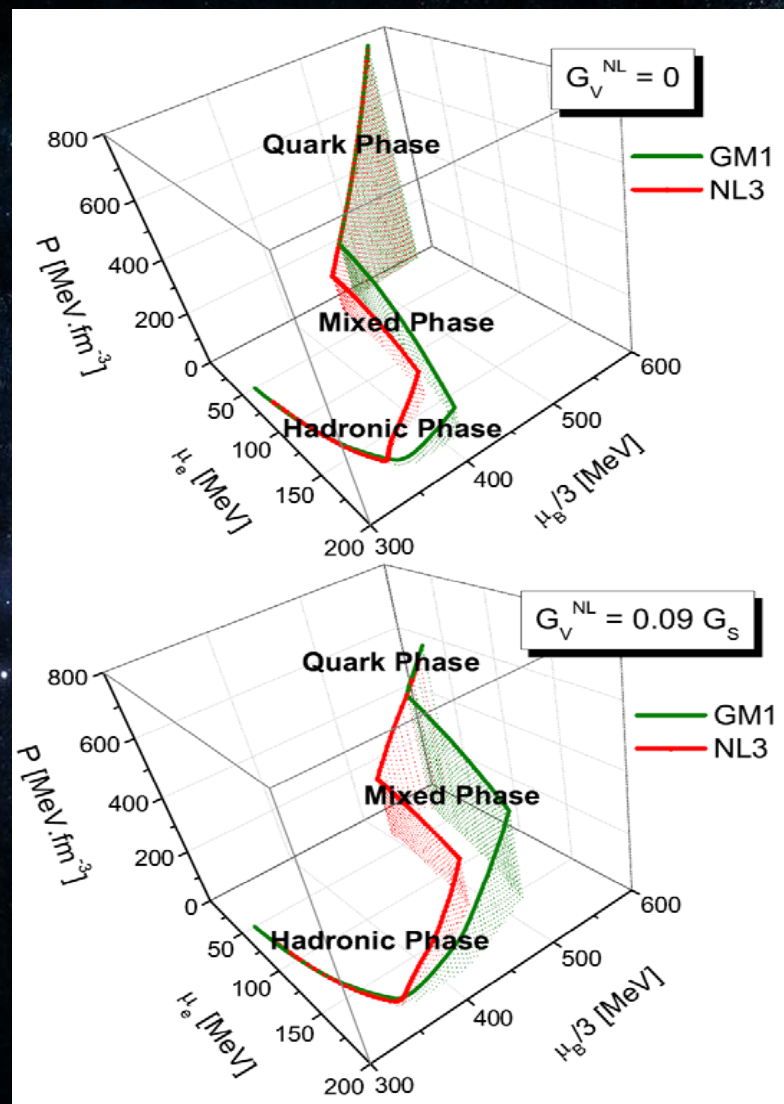
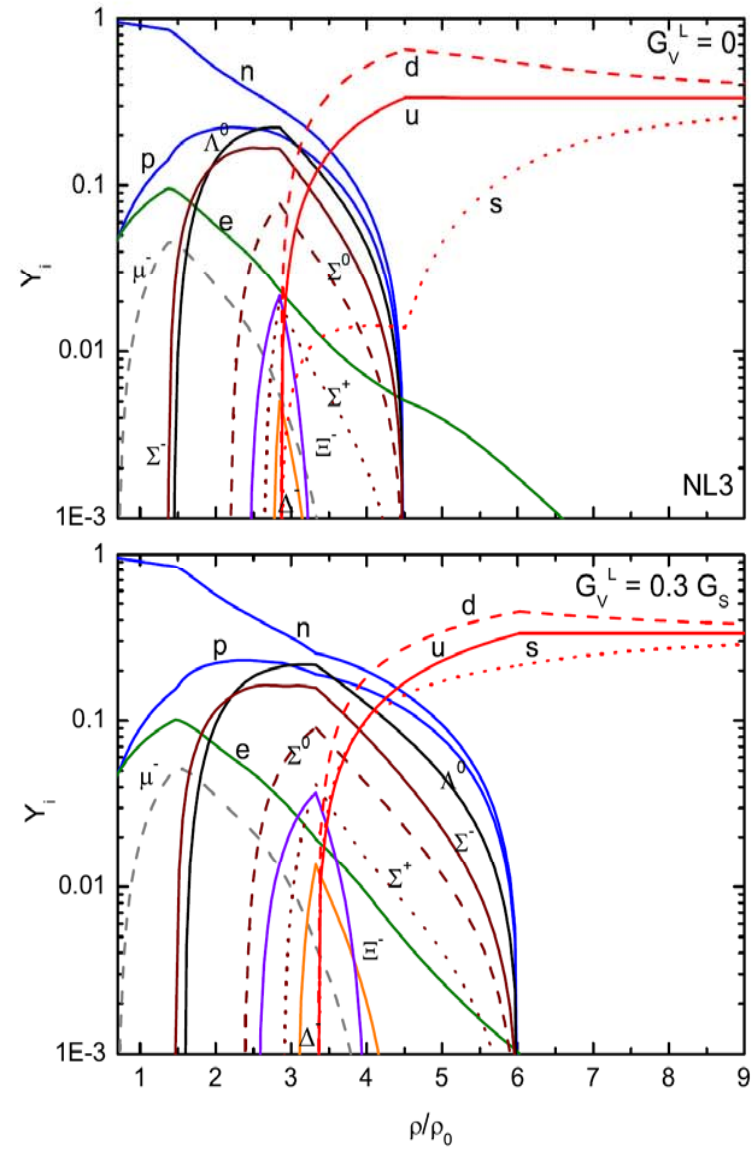
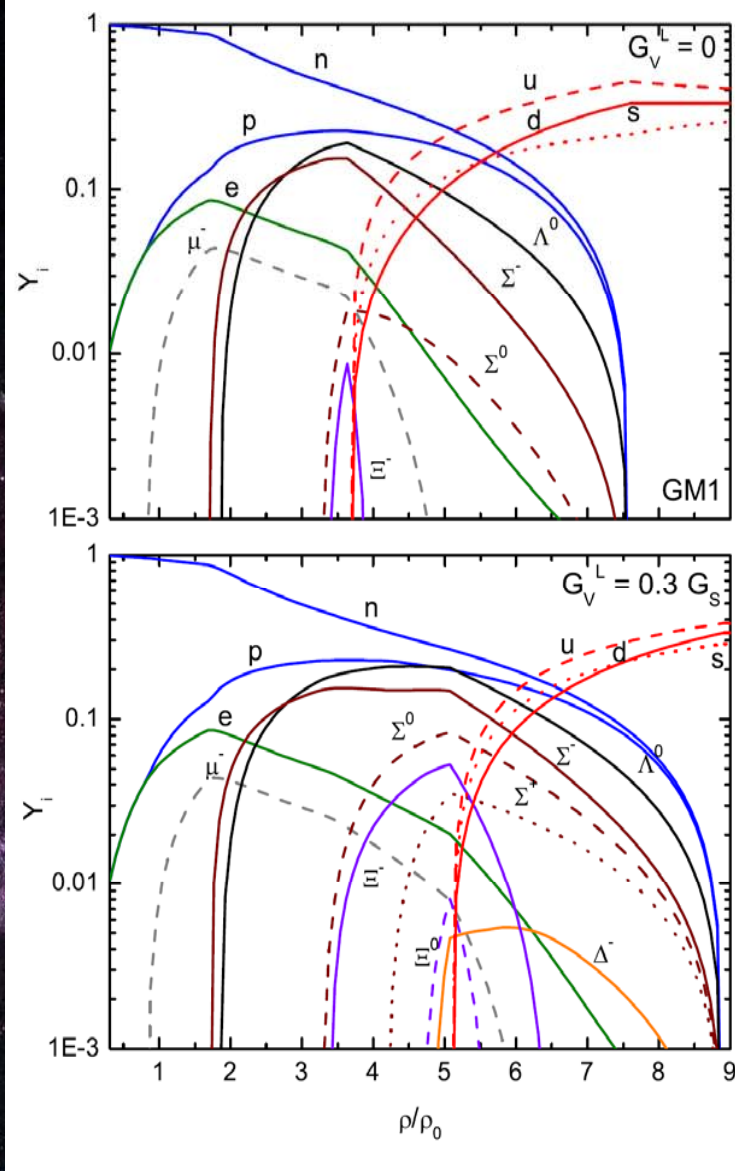
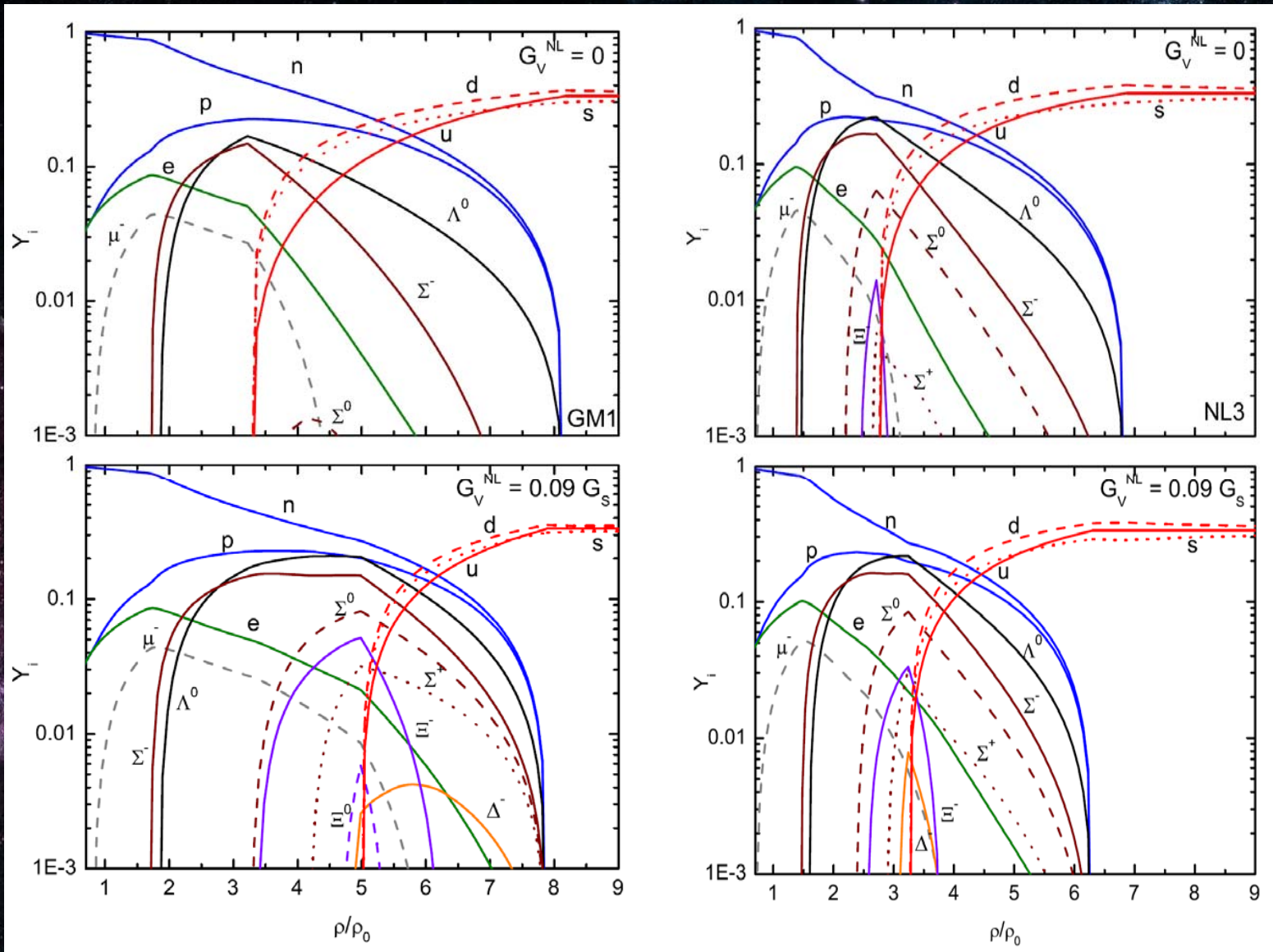


Figure 4. (Color online) Same as Fig. 3, but for the non-local NJL model, n3NJL, hadronic parametrizations GM1 and NL3, and vector repulsions  $G_V^{NL}/G_S = 0$  and  $G_V^{NL}/G_S = 0.09$ .

# Particle Population for local NJL model



# Particle Population for non-local NJL model



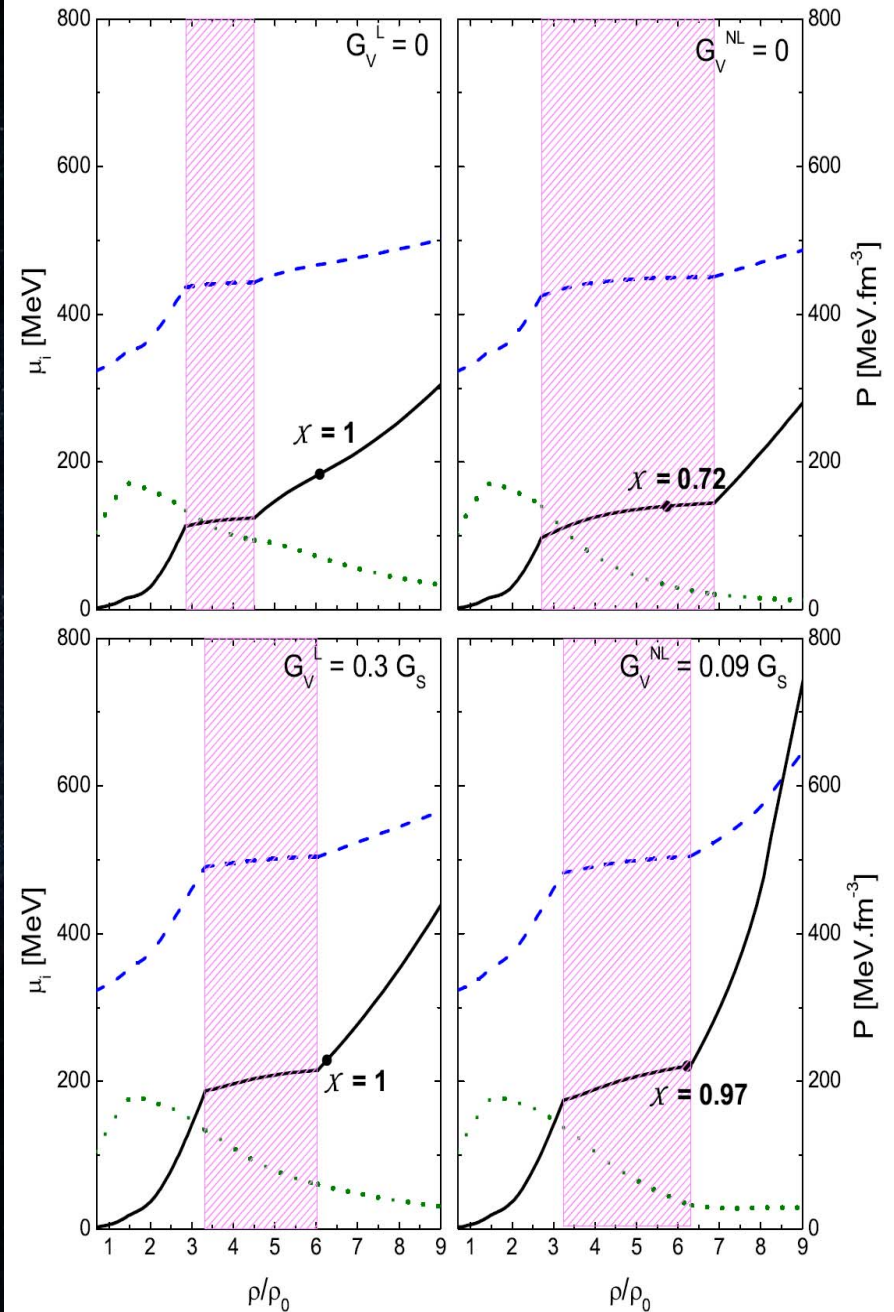
Pressure  $P$  (solid lines), baryonic chemical potential  $\mu_B$  (dashed lines), and electron chemical potential  $\mu_e$  (dotted lines) as a function of baryon number density in units of normal nuclear matter density,  $\rho_0 = 0.16 \text{ fm}^{-3}$  for parametrization NL3.

Table VI. Width of the mixed phase, central densities of the associated maximum-mass star of the QHS in the Local NJL model case.

$G_V^L$	Mixed phase ( $\rho_0$ )	Central density of $M_{\max}$ ( $\rho_0$ )
0 (GM1)	3.64 – 7.60	7.21
0.30 (GM1)	5.07 – 8.92	8.81
0 (NL3)	2.85 – 4.51	5.96
0.30 (NL3)	3.33 – 6.03	6.52

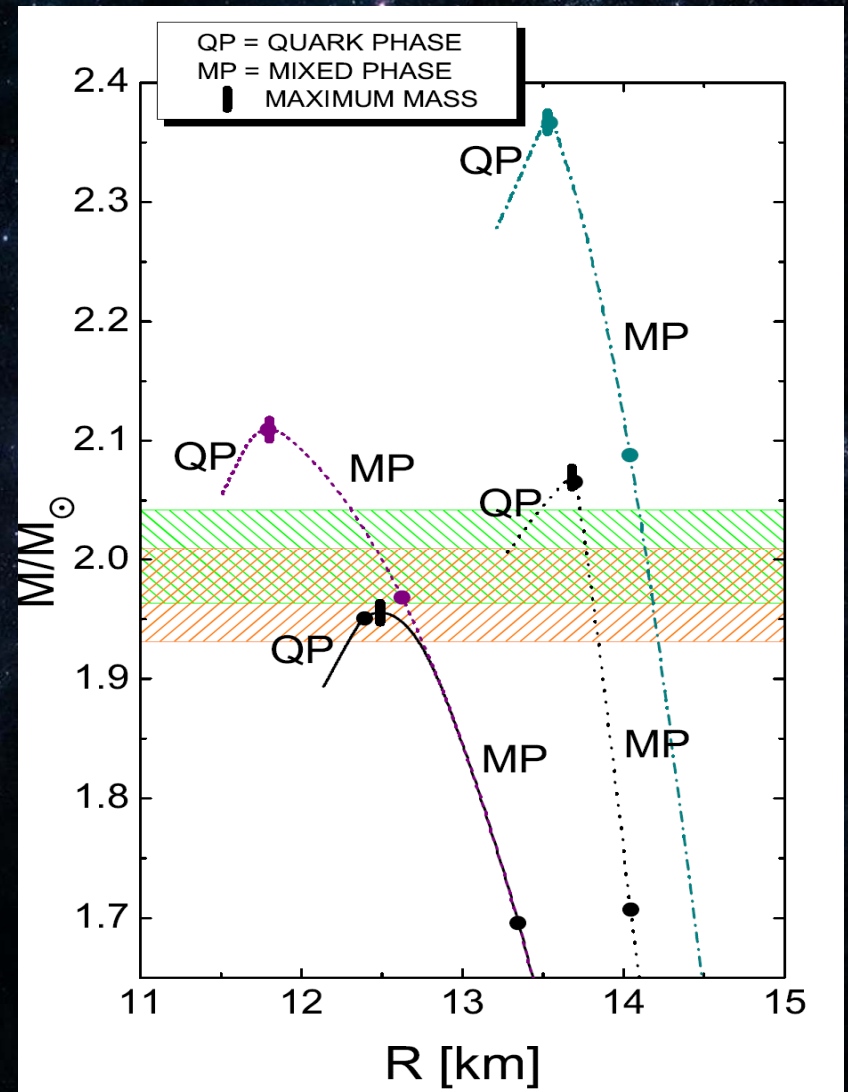
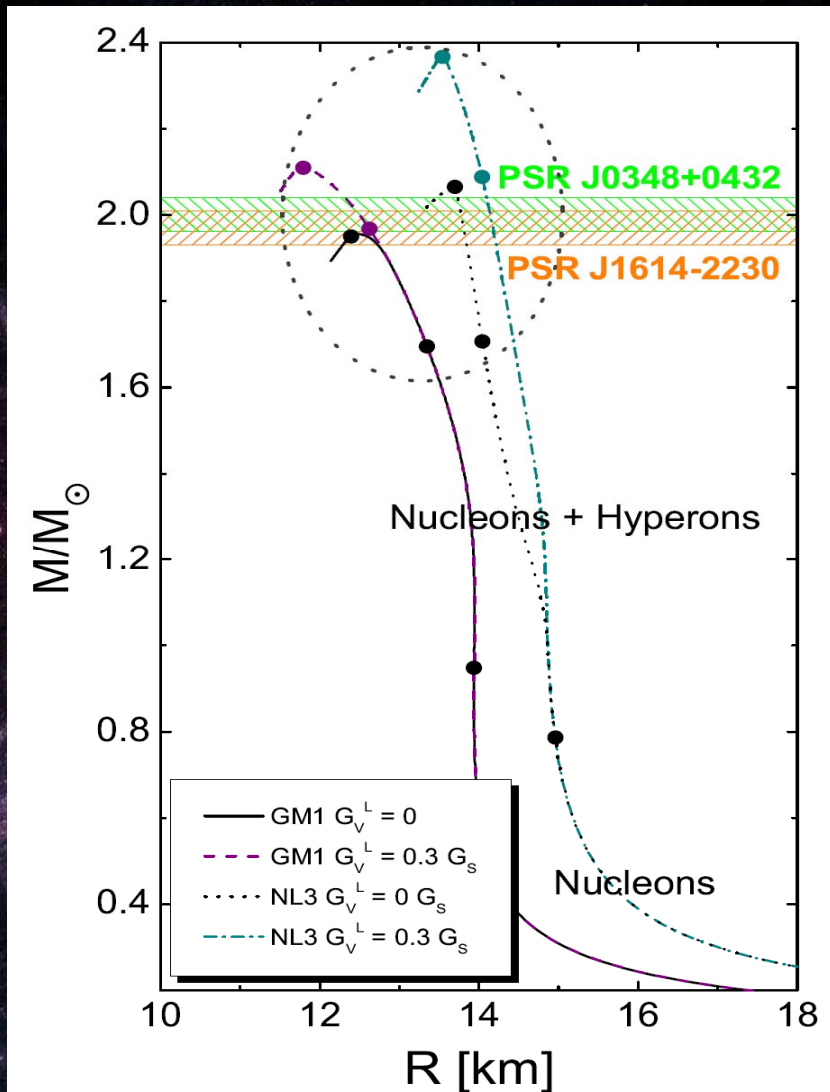
Table VII. Widths of the mixed phases and central densities of the associated maximum-mass stars for the non-local NJL model.

$G_V^{NL}$	Mixed phase ( $\rho_0$ )	Central density of $M_{\max}$ ( $\rho_0$ )
0 (GM1)	3.22 – 8.18	6.87
0.09 (GM1)	4.83 – 7.89	8.69
0 (NL3)	2.71 – 6.87	5.68
0.09 (NL3)	3.24 – 6.31	6.28





# Mass – Radius for local NJL model



# Mass – Radius relation for non-local NJL model

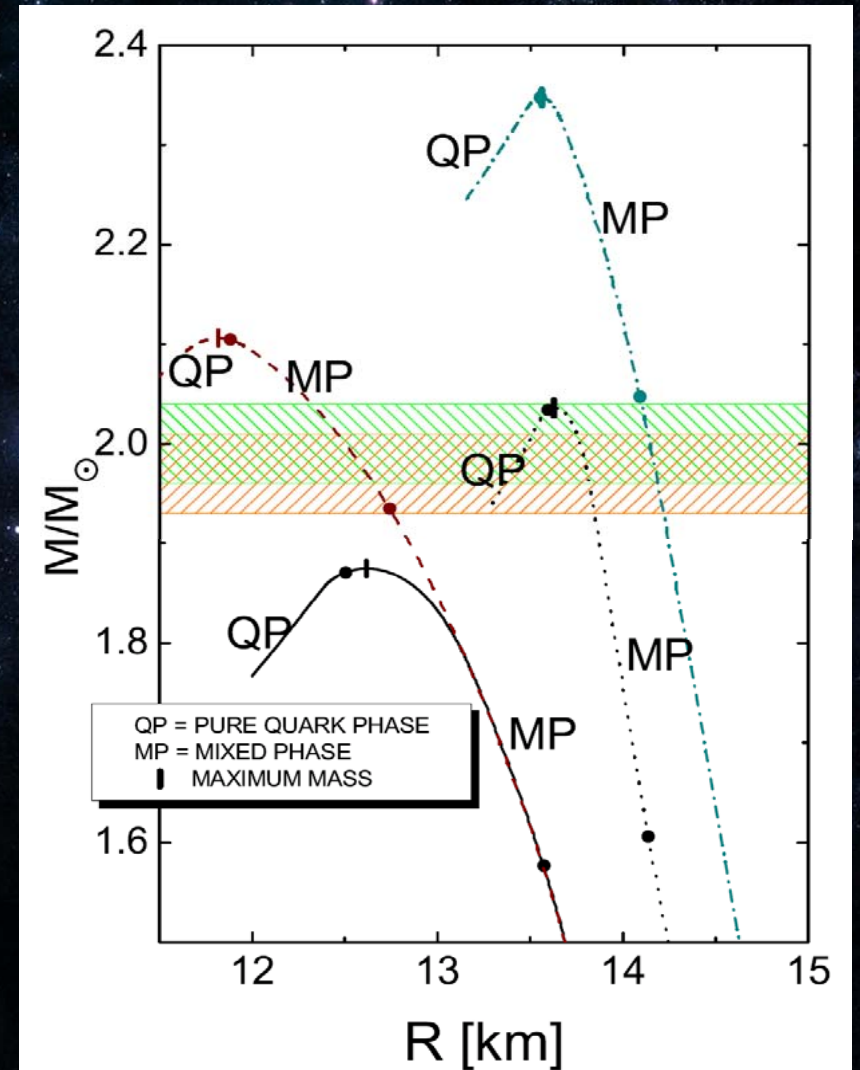
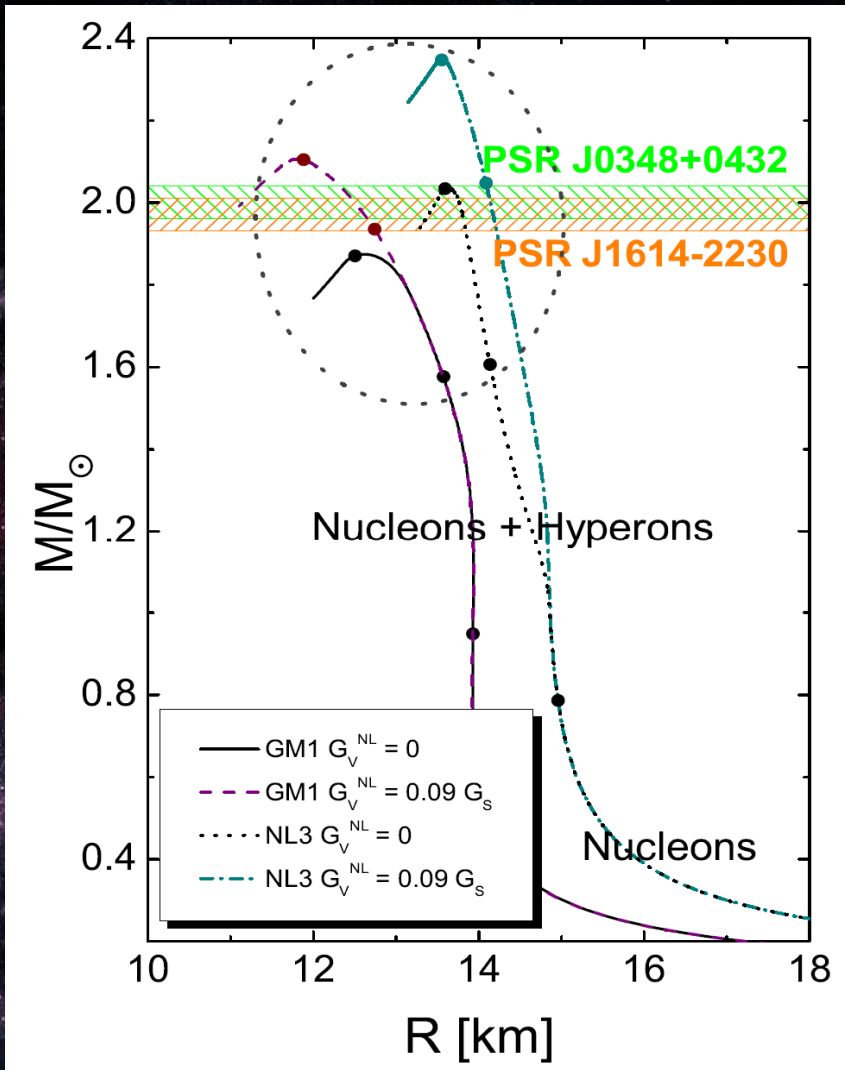


Table VIII. Maximum masses and radii of neutron stars made of quark-hybrid matter for different vector repulsion ( $G_V/G_S$ ).

NJL Model	$G_V/G_S$	$R_{\max}$ (km)	$M_{\max}/M_{\odot}$
Local	0	12.49	1.96
GM1	0.30	11.80	2.11
Local	0	13.68	2.07
NL3	0.30	13.53	2.37
Non-local	0	12.62	1.87
GM1	0.09	11.81	2.11
Non-local	0	13.62	2.04
NL3	0.09	13.56	2.35

# Summary

- We have used a non-local 3-flavor NJL model to modelate the quark matter and a non-linear Walecka model for the hadronic phase.
- The inclusion of the vector interaction is crucial for the stiffens of the EoS and the consequent increase of then M-R relationship.
- According to our results, high-mass Neutron Stars such as PSR J1614-2230 and J0348+0432 may contain a mixed phase of quarks and hadrons in their cores.

## Outlook

- **Extension to finite temperature : protoneutron stars.**
- **Color Superconductivity**



**Thank you very much  
for your attention!**

Gustavo A. Contrera