

# Principios de analise 1:

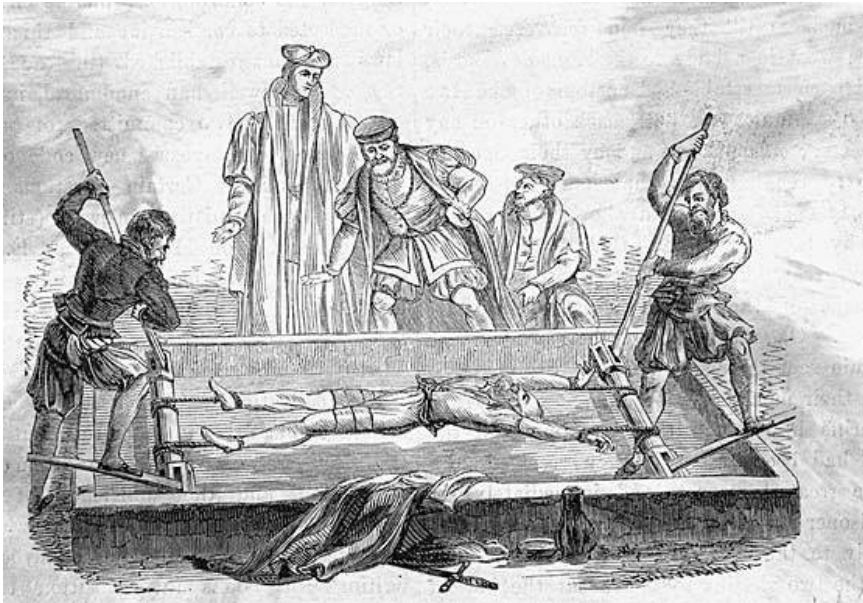
## Macro-experimental

(em Ingles: 'heat and beat')

Modelos de continuum-  
stress vs strain,  
fluxos de calor e ions,  
campos electricos e magneticos



# Stress-Strain Relations- apply a force, measure the deformation



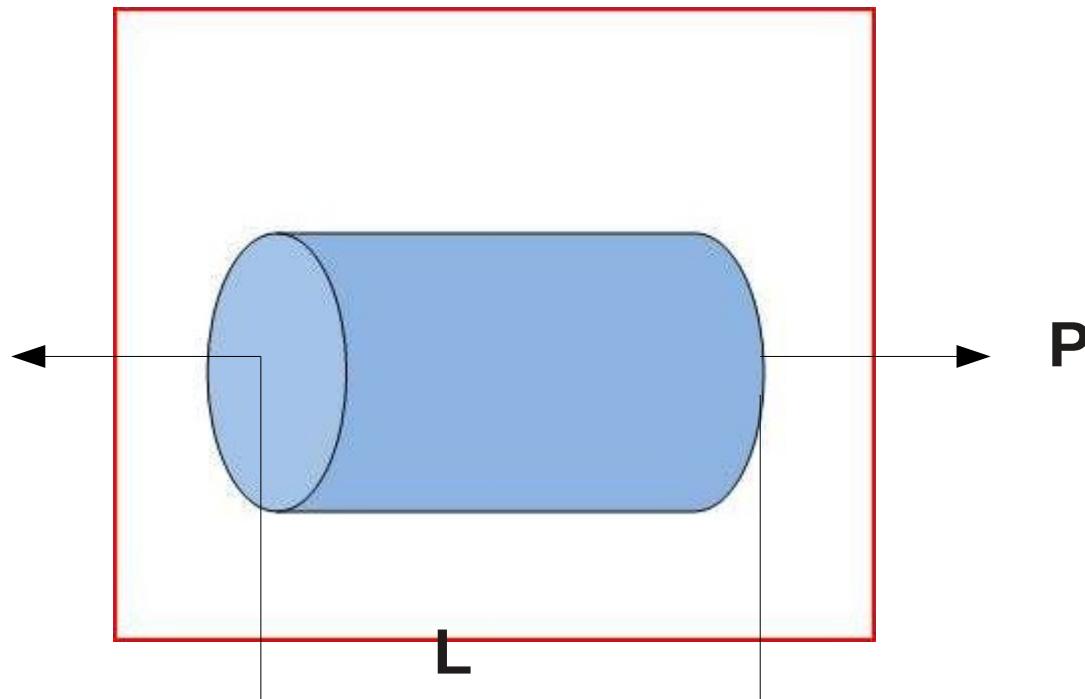
Medieval Model



Modern Model

A basic ingredient in the study of the mechanics of deformable bodies is the resistive properties of materials. These properties relate the stresses (**push/pull/shear/twist**) to the strains (**deformations**).

In the **tensile test**, a load is applied along the longitudinal axis of a circular test specimen. The applied load and the resulting elongation of the member are measured, until the specimen breaks.



**Load-deformation data obtained from tensile and/or compressive tests depend on the specimen geometry. However, loads and deformations may be converted to size-independent stresses and strains. Thus**

$$\sigma = P/A$$

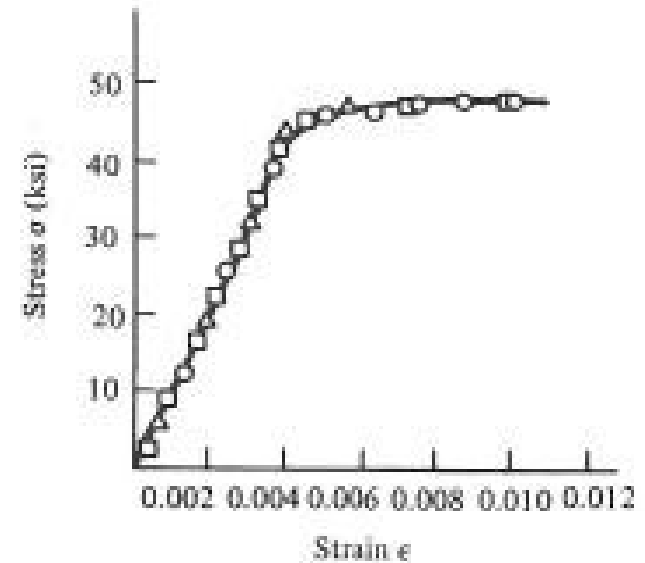
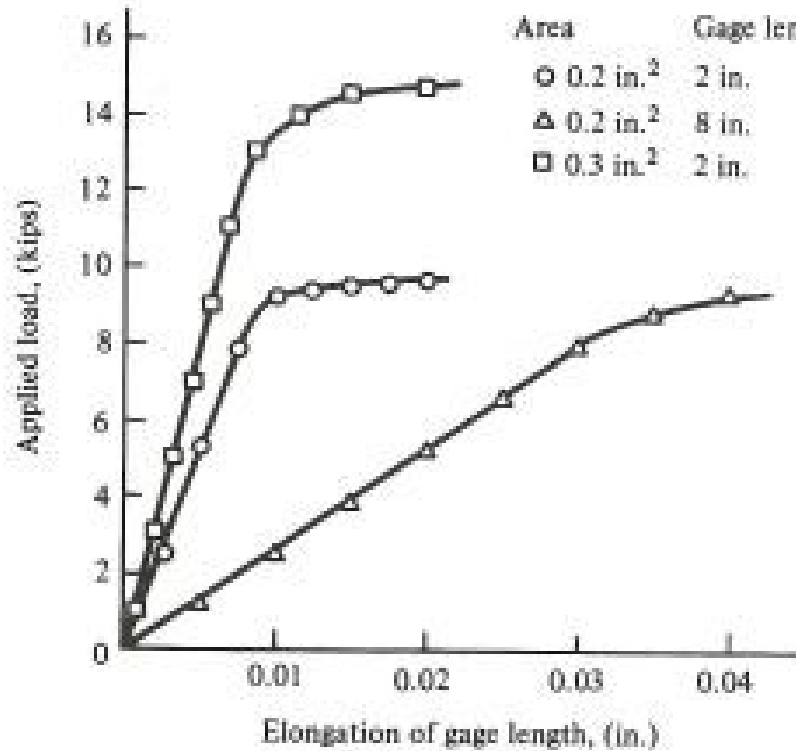
$$\epsilon = \delta/L$$

- $\sigma$  = normal stress on a plane perpendicular to the longitudinal axis of the specimen  
1 Gigapascal =  $10^9$  N/m<sup>2</sup> ~  $10^4$  atmosphere
- P = applied load
- A = original cross sectional area
- $\epsilon$  = normal strain in the longitudinal direction  
dimensionless
- $\delta$  = change in the specimen's gage length
- L = original gage length
- $K = \sigma / \epsilon$  == Young's modulus (Gpa)===stiffness===spring constant

# 2017-T451 Aluminum Alloy

## Load-deformation data

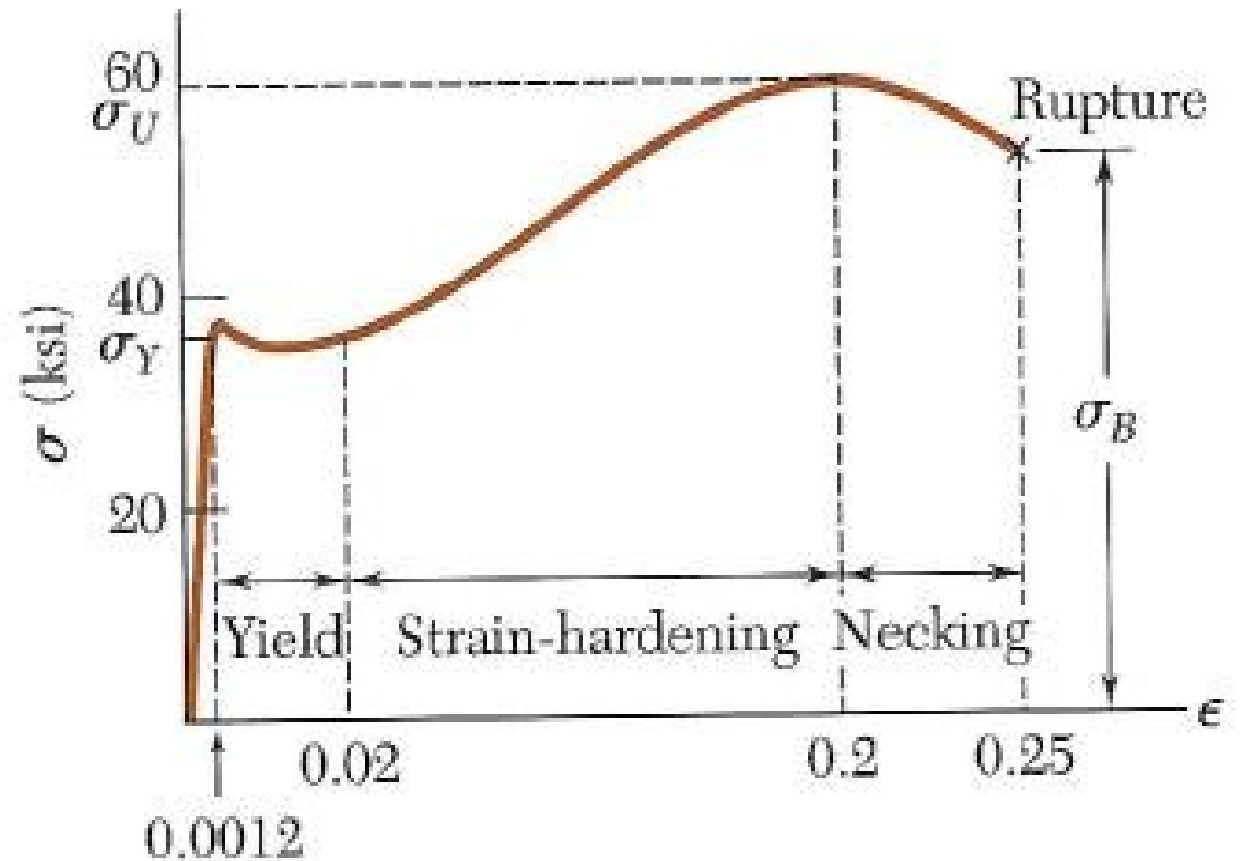
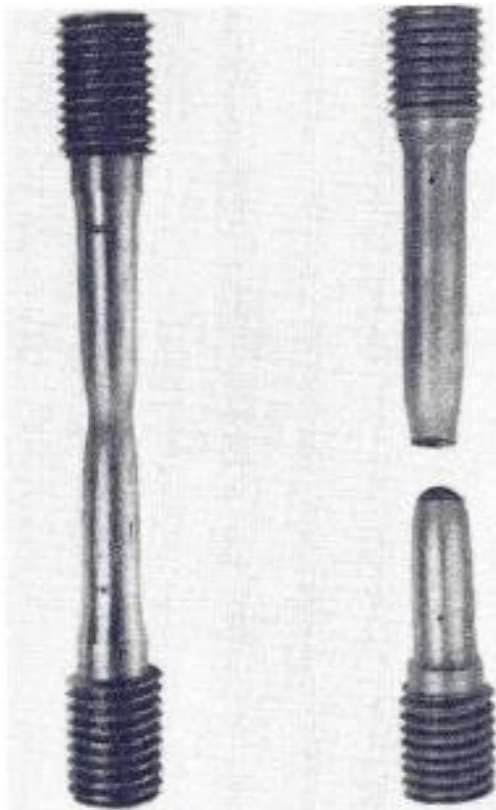
## Stress-strain data



Load vs deformation  
for three specimens

Mapped onto common  
Stress vs Strain map

Stress vs Strain of steel rod shows:  
Hooke linear region, yield region,  
strain-hardening region, necking and failure



(a) Low-carbon steel

# Ductile vs Brittle?

- Ductile Material – Materials that are capable of undergoing large strains (at normal temperature) before failure. An advantage of ductile materials is that visible distortions may occur before the loads become too large. Ductile materials are also capable of absorbing large amounts of energy prior to failure.
- Ductile materials include mild steel, aluminum and some of its alloys, copper, magnesium, nickel, brass, bronze and many others.
- Brittle Material – Materials that exhibit very little inelastic deformation. In other words, materials that fail in tension at relatively low values of strain are considered brittle.
- Brittle materials include concrete, stone, cast iron, glass and plaster.
- 

HDPE tensile test

stainless steel tensile test

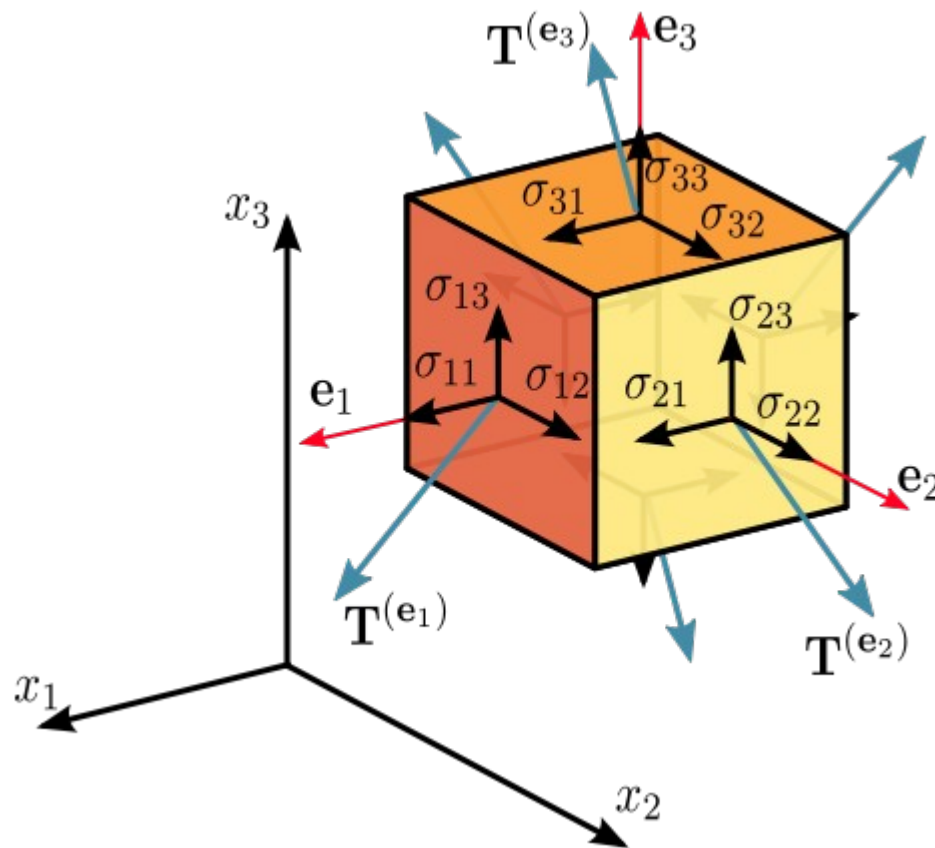
# Longitudinal and Transverse Stress



A complete description of the mechanical load on a solid requires three longitudinal stress components and six transverse (shear) components.

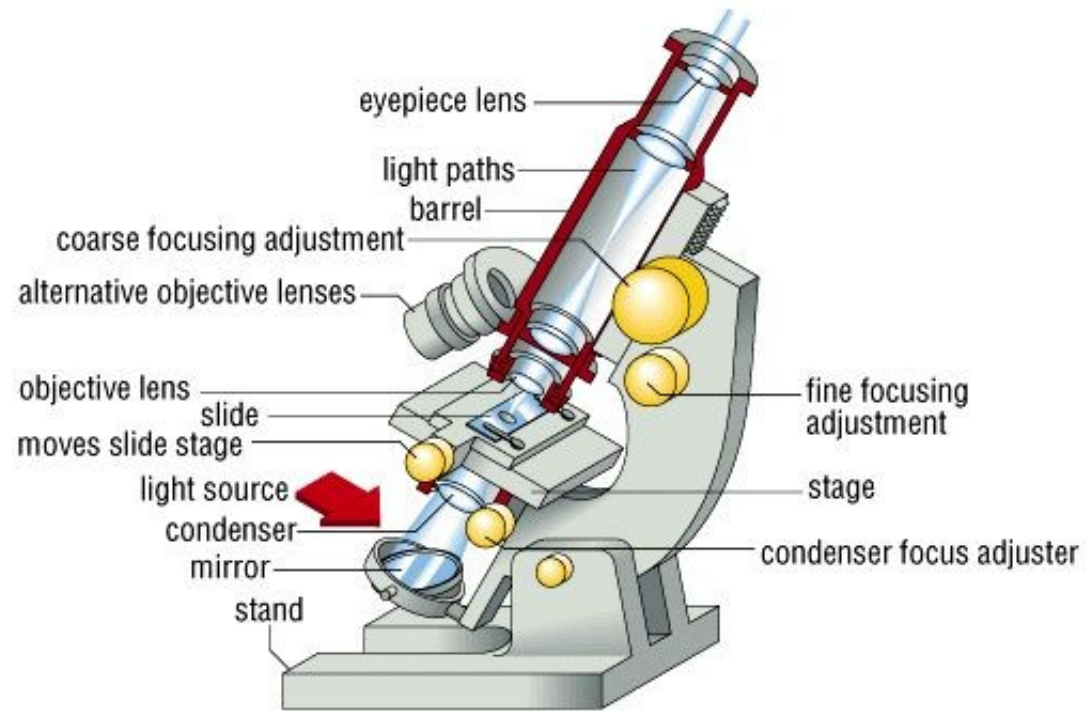
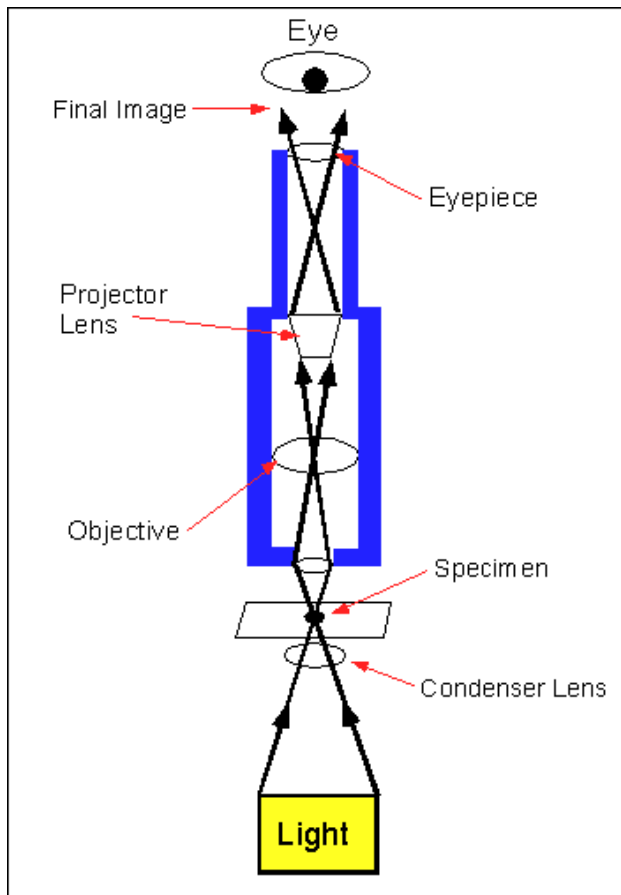


In Cauchy's world stress is described by a  $3 \times 3$  matrix  $[\sigma_{ij}]$  which causes the  $3 \times 3$  strain response  $[\varepsilon_{ij}]$

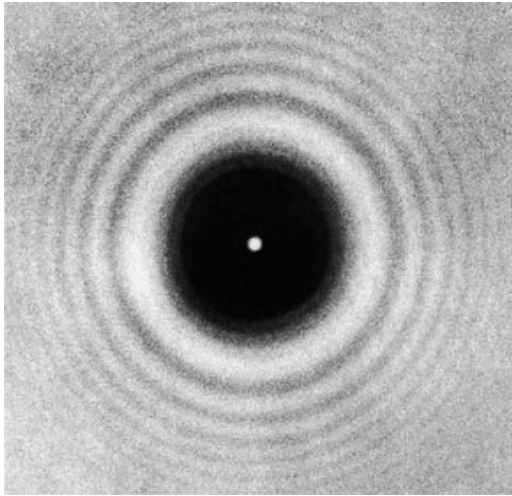


## Princípios de análise 2:

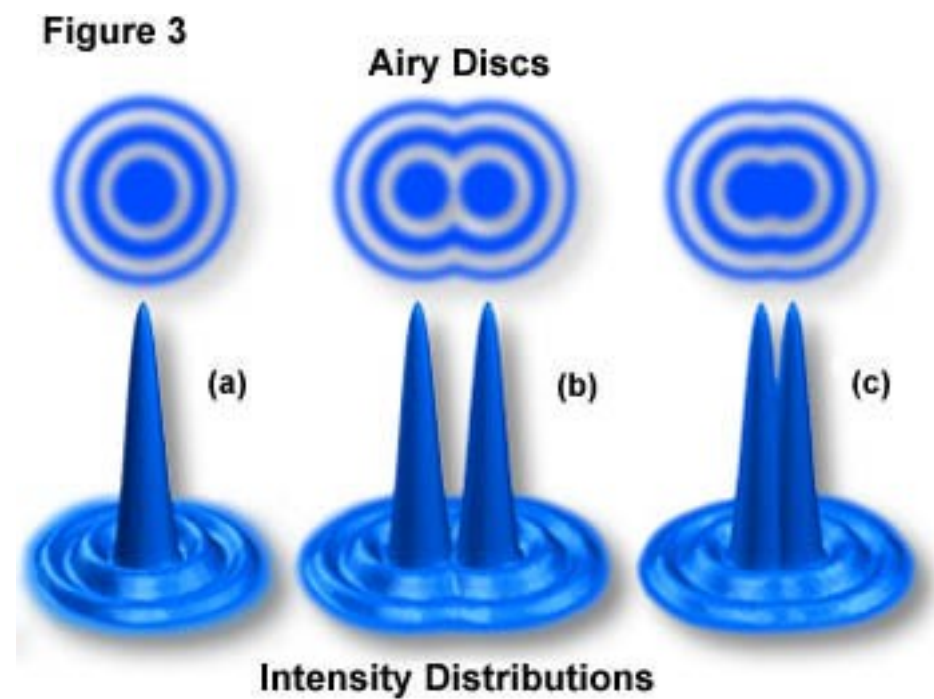
Micro-experimental:  
microscopia ótica, ultravioleta & infravermelho,  
ultrasom,  
raios-X & gamma...



**Traditional compound optical microscope** usually has two sets of glass lenses and an eyepiece. The first true compound microscope was developed in 1609 in the Netherlands by Zacharias Janssen. Modern compound light microscopes, under optimal conditions, can magnify an object from 1000X to 2000X (times) the specimens original diameter. **Fluorescence microscopy** makes use of fluorescent dyes to illuminate samples, or to highlight the presence of particular substances within a sample. Various illumination systems are also used to highlight details.



Experimental diffraction pattern around a dark disk. Hey, what's that bright dot in the middle?



Schematic intensity field for one and two (nearby) sources seen through microscope/telescope

The observation of sub-wavelength structures with microscopes is difficult because of the **Abbe diffraction limit**. **Ernst Abbe** found in 1873 that light with wavelength  $\lambda$ , traveling in a medium with refractive index  $n$  and converging to a spot with angle  $\theta$  will make a spot with radius

$$d = \lambda / 2(n \sin \theta)$$

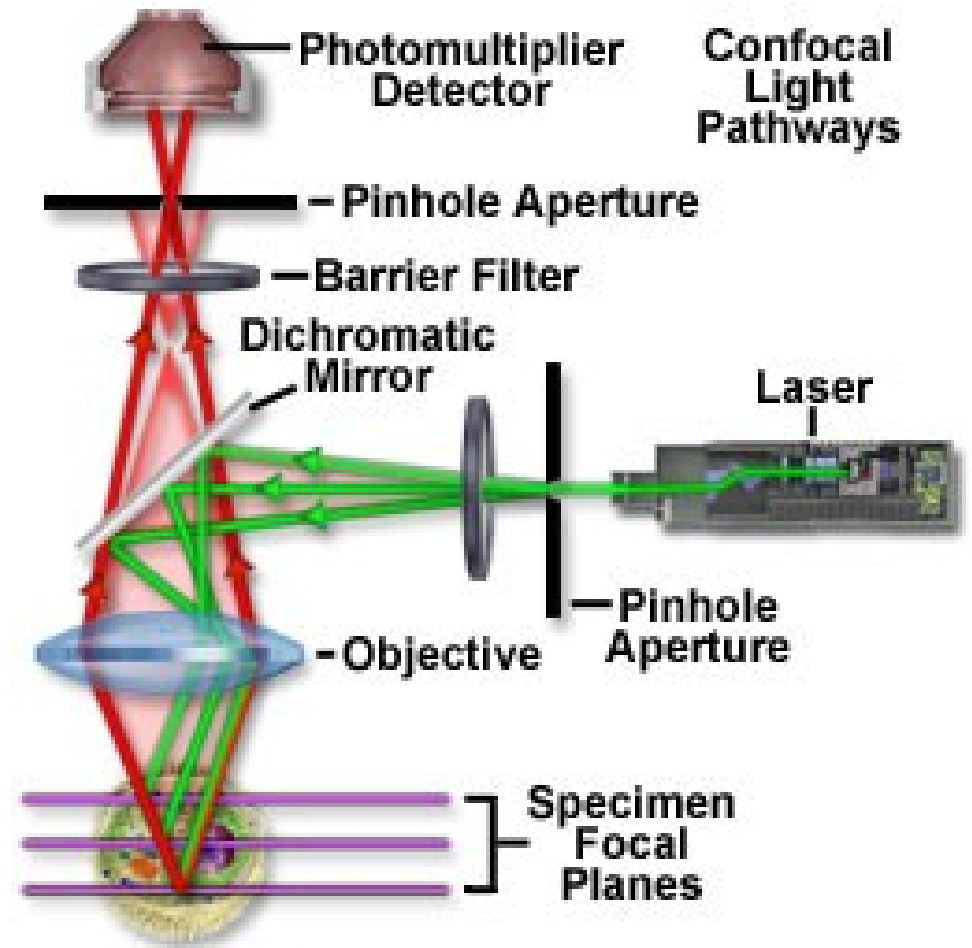
The denominator is called the **numerical aperture** and can reach about 1.4 in modern optics, hence the Abbe limit is roughly  $d = \lambda / 2$ . With green light around 500nm the Abbe limit is 250nm which is large compared to most nanostructures or biological cells which have sizes on the order of  $1\mu\text{m}$  and internal organelles which are much smaller



**FluoView™ FV1000  
Scanning Unit  
with the IX81 Inverted  
Microscope**

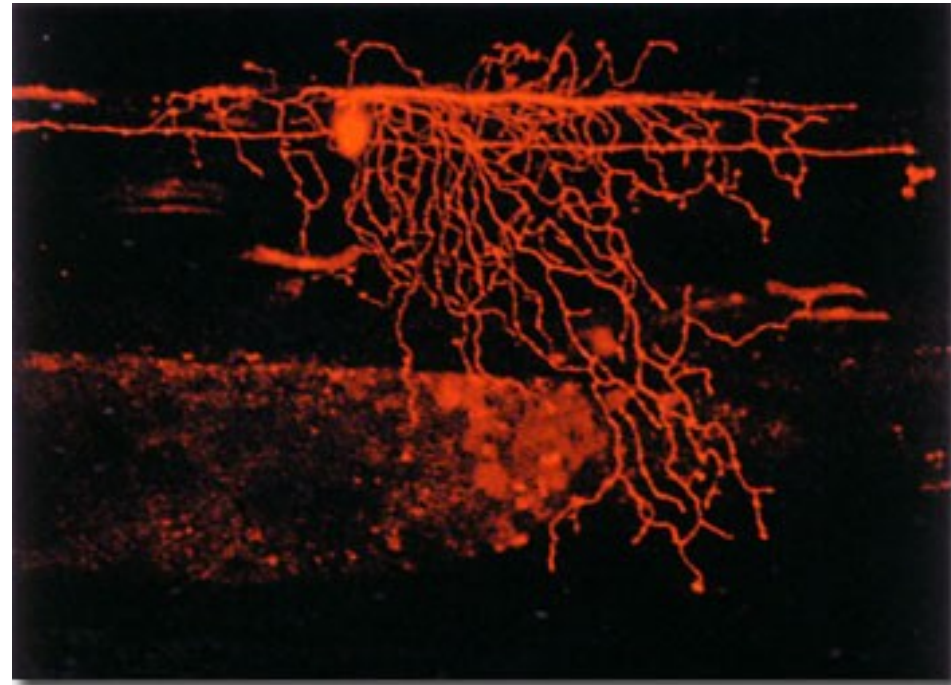
FluoView™ FV1000 Confocal Laser Scanning Biological Microscope - A leader in the next generation of live cell confocal imaging systems, the FV1000 features simultaneous laser light stimulation and imaging by incorporating two laser scanners in a single compact design. Synchronization of these two functions ensures that cellular reactions occurring immediately following or during stimulation are not overlooked, a key feature in microscopes designed for FRAP, FLIP, and photo activation.

Laser scanning confocal microscopy represents one of the most significant advances in optical microscopy ever developed, primarily because the technique enables visualization deep within both living and fixed cells and tissues and affords the ability to collect sharply defined optical sections from which three-dimensional renderings can be created. The principles and techniques of confocal microscopy are becoming increasingly available to individual researchers as new single-laboratory microscopes are introduced. Development of modern confocal microscopes has been accelerated by new advances in computer and storage technology, laser systems, detectors, interference filters, and fluorophores for highly specific targets.



## Fluorescent Protein Expression in Zebrafish Embryos

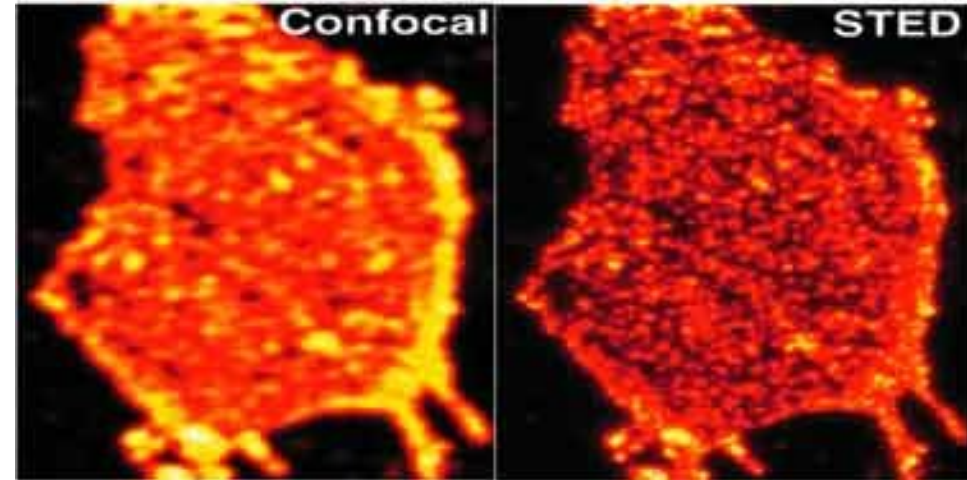
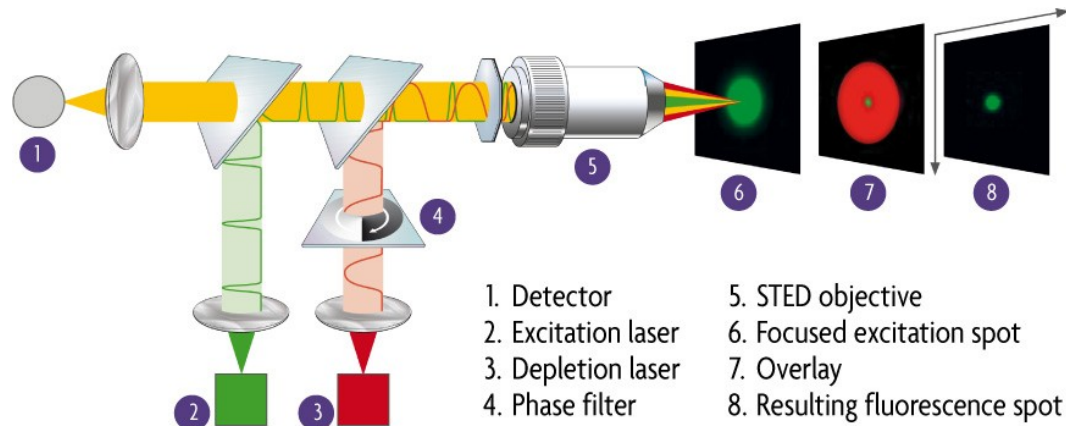
Spectral variants of the green fluorescent protein (**GFP**) are quite useful for double or triple labeling experiments or when targeting fluorescence expression with a particular laser system. The confocal image presented below is a three-dimensional volume render made from 5-micrometer serial optical sections of a zebrafish embryo labeled with a red fluorescent protein (**dsRED**). The image was provided by Yasuhiro Kamei and Shunsuke Yuba of the Institute for Molecular and Cellular Biology at Osaka University, in Japan.



Try this:  
[confocal\\_microscope\\_simulator](#)



A lot of tricks have been developed fairly recently, to get around the diffraction limit... one example: STED

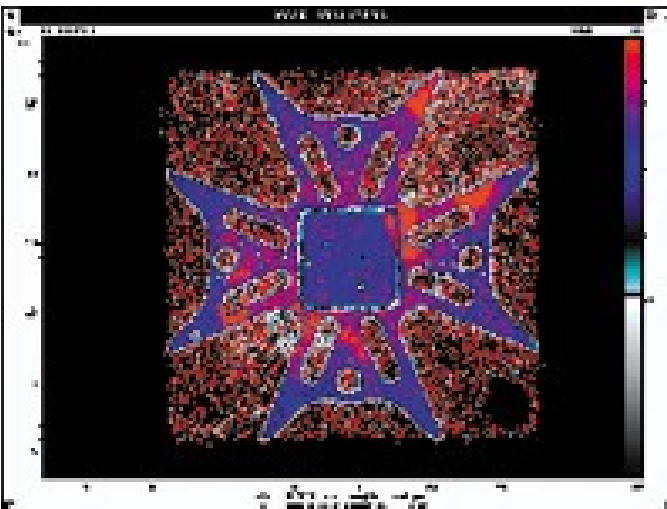
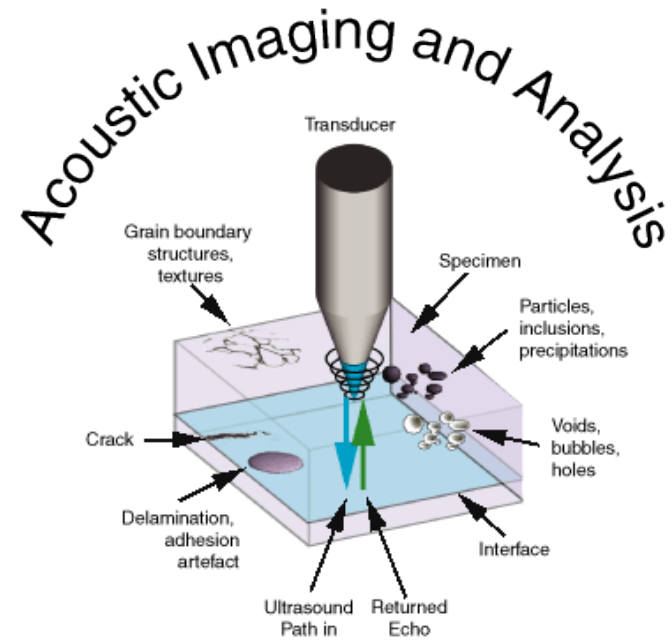


Resolution comparison of confocal versus STED-microscopy; plasma, membrane patches immuno-stained against the SNARE protein SNAP25 secondary antibody labeled with Atto 532-NHS; Emission 540-570 nm, STED at 615 nm. The confocal image was recorded by simply turning off the STED beam with no other changes.

**Stimulated emission depletion** is a simple example of how higher resolution surpassing the diffraction limit is possible, but it has major limitations. STED is a fluorescence microscopy technique which uses a combination of light pulses to induce fluorescence in a small sub-population of fluorescent molecules in a sample. Each molecule produces a diffraction-limited spot of light in the image, and the center of each of these spots corresponds to the location of the molecule. As the number of fluorescing molecules is low the spots of light are unlikely to overlap and therefore can be placed accurately. This process is then repeated many times to generate the image. [Stefan Hell](#) of the Max Planck Institute for Biophysical Chemistry was awarded the 10th German Future Prize in 2006 for his development of the STED microscope.



Ultrasound- piezoelectric drivers/receiver arrays operating over 1-100 Mhz for non-destructive imaging. Bats, dolphins, etc. use the band 20-100 KHz for imaging. Medical applications are 1-20 Mhz.



Ultrasound permits looking 'below the surface' on many scales- from microchips, to babies, to aircraft wings, to oil ducts

# Modelos na escala de microns ate metros – analise de elemento finitos; o bom e velho Newton

## **Syllabus for an online course in continuum mechanics@Wikiversity**

Mathematical Preliminaries

Set notation

Functions

Vectors

Matrices

Tensors

Useful tensor algebra identities

Useful relations between tensors and vectors

Curl of the gradient of a vector

Relations between surface and volume integrals

Leibniz formula in one dimension

Leibniz formula in three dimensions

Partial differential equations

Variational calculus

Kinematics

Motion, displacement, velocity, acceleration

Strains and deformations

Polar decomposition

Spectral decompositions of kinematic quantities

Volume change and area change

Time derivatives and rate quantities

Objectivity of kinematic quantities

Stress measures and stress rates

Stress measures

Deviatoric and volumetric stress

Objective stress rates

Balance laws

Governing equations and thermodynamics

Balance of mass

Balance of linear momentum

Balance of angular momentum

Balance of energy

Clausius-Duhem inequality

Constitutive relations

Thermoelasticity

Relation between Cauchy stress and Green strain

Maxwell relations for thermoelasticity

Balance of energy

Clausius-Duhem inequality

Specific heat relations

Nonlinear Elasticity

Plasticity

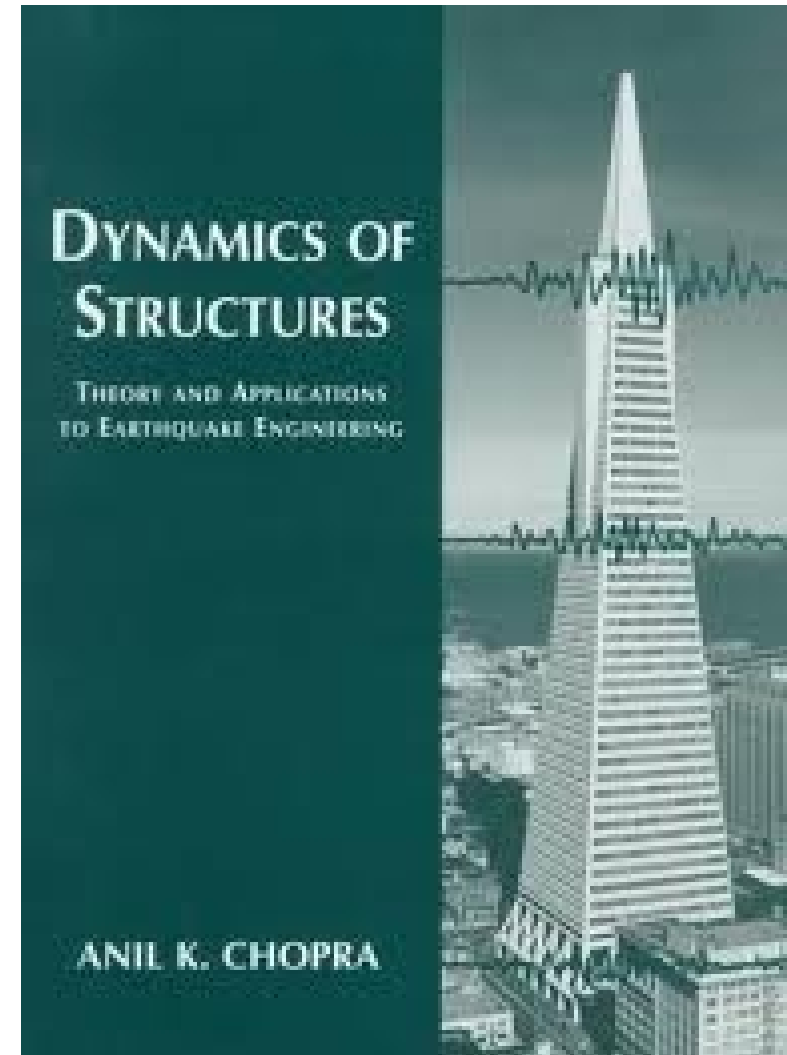
Viscoplasticity

Viscoelasticity.

Principles of continuum mechanics appear simple, but applications to real-world materials problems lead to subtle nonlinear mathematics, and eventually finite-element computer models



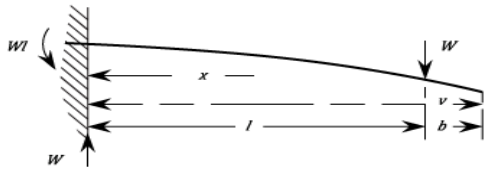
Glacier flows determine in part pace of global warming and sea-level rise. Their dynamics are partially understood.



Try This: [SF\\_Oakland bay bridge](#)

## Even the simplest beam-deflection problem is highly nonlinear:

The out-of-plane displacement  $w$  of a beam is governed by the **Euler-Bernoulli Beam Equation**,



$$\frac{d^2}{dx^2} \left[ EI \frac{d^2 w}{dx^2} \right] = p$$

where  $p$  is the distributed loading (force per unit length) acting in the same direction as  $y$  (and  $w$ ),  $E$  is the Young's modulus of the beam, and  $I$  is the area moment of inertia of the beam's cross section.

If  $E$  and  $I$  do not vary with  $x$  along the length of the beam, then the beam equation simplifies to,



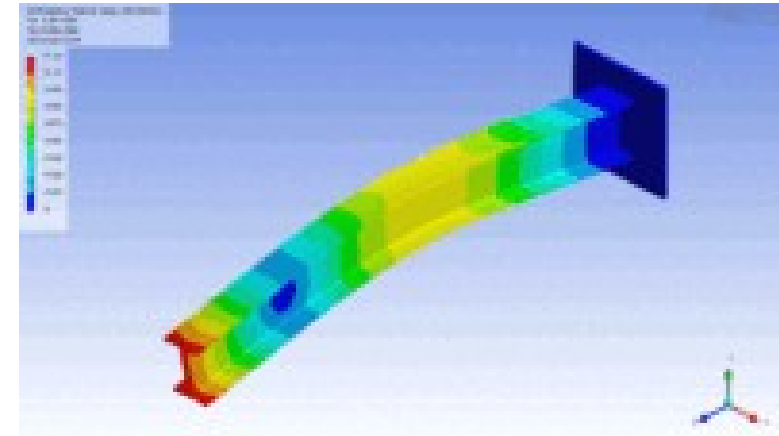
$$EI \frac{d^4 w}{dx^4} = p$$



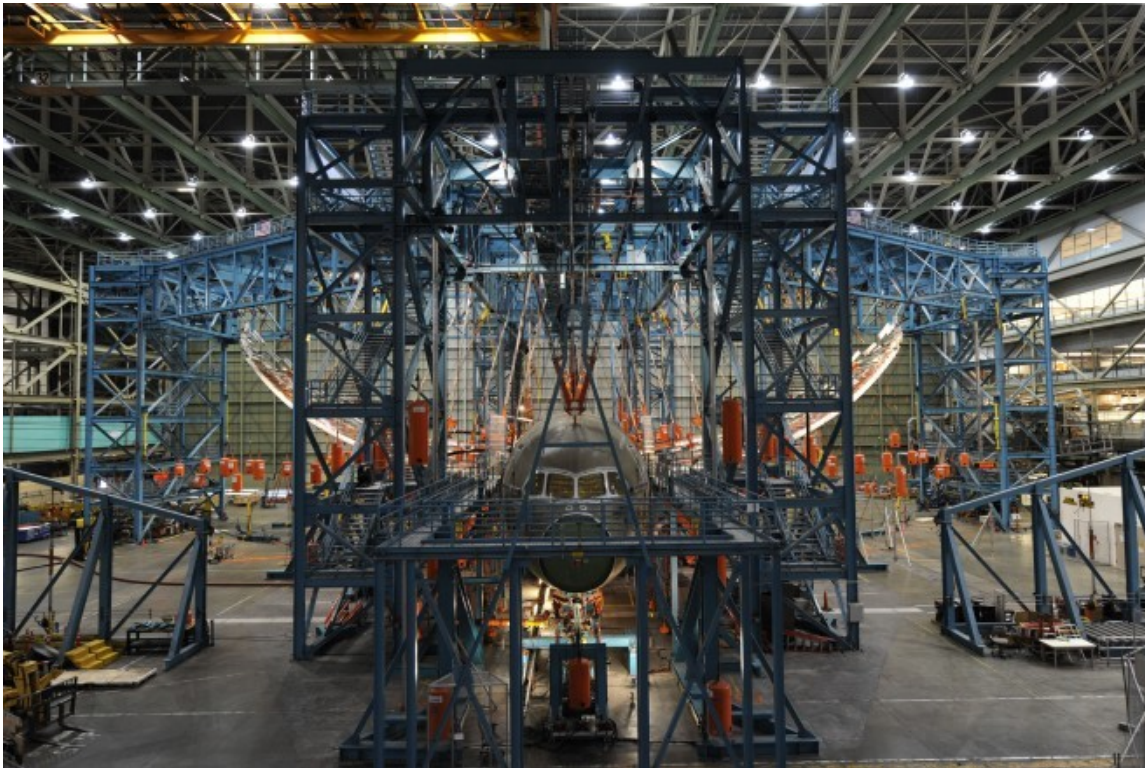
Of course, time-dependent stress-strain relations are more fun!!

$$\frac{\partial^2}{\partial x^2} \left( EI \frac{\partial^2 w}{\partial x^2} \right) = -\mu \frac{\partial^2 w}{\partial t^2} + q(x)$$

Time-dependent Euler-Bernoulli equation for  
A loaded beam



Finite element computer models  
And graphics are essential tools



Boeing 787 wings at  
150% design overload

# What is the Finite Element Method?

The finite element method (FEM) is the dominant discretization technique in structural mechanics. The basic concept in the physical interpretation of the FEM is the subdivision of the mathematical model into disjoint (non-overlapping) components of simple geometry called finite elements or elements for short. The response of each element is expressed in terms of a finite number of degrees of freedom characterized as the value of an unknown function, or functions, at a set of nodal points.

The response of the mathematical model is then considered to be approximated by that of the discrete model obtained by connecting or assembling the collection of all elements. The disconnection-assembly concept occurs naturally when examining many artificial and natural systems. For example, it is easy to visualize an engine, bridge, building, airplane, or skeleton as fabricated from simpler components. Unlike finite difference models, finite elements do not overlap in space.

FEM model of femur; coarse grid for whole body mechanics, fine grid for prosthesis design/simulation

